



Heterostructure Epitaxy for fondamental research

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Outline



1. A bit of history

Electron mean-free path

2. A few experiments on mesoscopic transport

Phase coherence

3. Light-Matter interaction

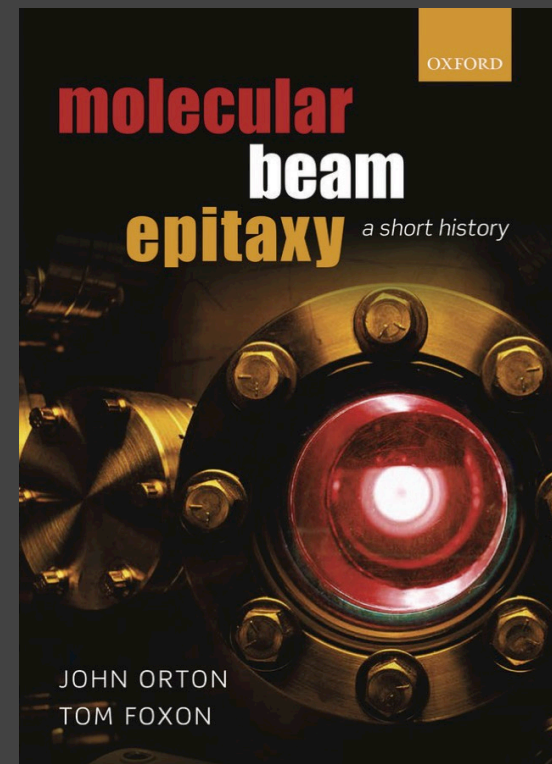
Exciton, polariton, quantum light

A bit of History



a “Chicken or the Egg” question !

Fundamental research drove MBE development
or
MBE development drove new fundamental research?

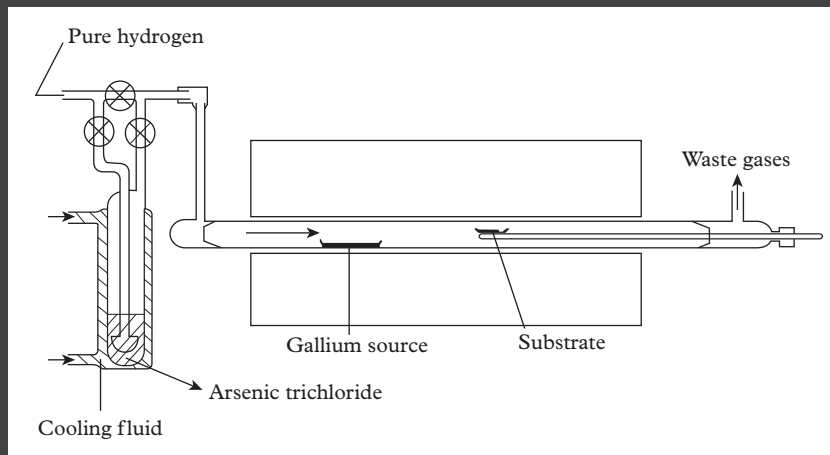


Early epitaxial techniques

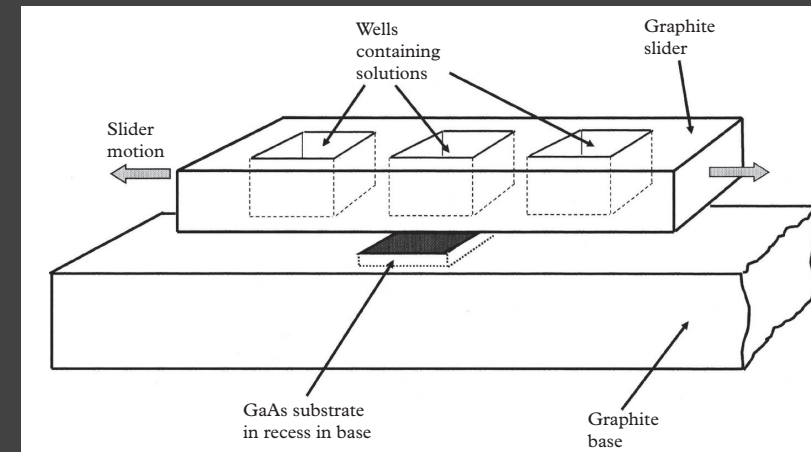
50's: tremendous improvement in single crystal quality

60's: first epitaxial techniques

VPE



LPE



VPE : mostly homoepitaxy, with dopant control (transistors, Gunn diode)
LPE : alloy epitaxy (AlGaAs), and then first heterostructures (lasers)

Very poor control of the layer thickness ($\sim \mu\text{m}$)

The Esaki and Tsu proposal in 1970



Superlattice and Negative Differential Conductivity in Semiconductors*

Abstract: We consider a one-dimensional periodic potential, or “superlattice,” in monocrystalline semiconductors formed by a periodic variation of alloy composition or of impurity density introduced during epitaxial growth. If the period of a superlattice, of the order of 100\AA , is shorter than the electron mean free path, a series of narrow allowed and forbidden bands is expected due to the subdivision of the Brillouin zone into a series of minizones. If the scattering time of electrons meets a threshold condition, the combined effect of the narrow energy band and the narrow wave-vector zone makes it possible for electrons to be excited with moderate electric fields to an energy and momentum beyond an inflection point in the $E-k$ relation; this results in a negative differential conductance in the direction of the superlattice. The study of superlattices and observations of quantum mechanical effects on a new physical scale may provide a valuable area of investigation in the field of semiconductors.

IBM J Res Dev 14, 61 (70)

The Esaki and Tsu proposal



Entering the quantum regime

Building heterostructures with characteristic size lower than the electron mean-free path λ

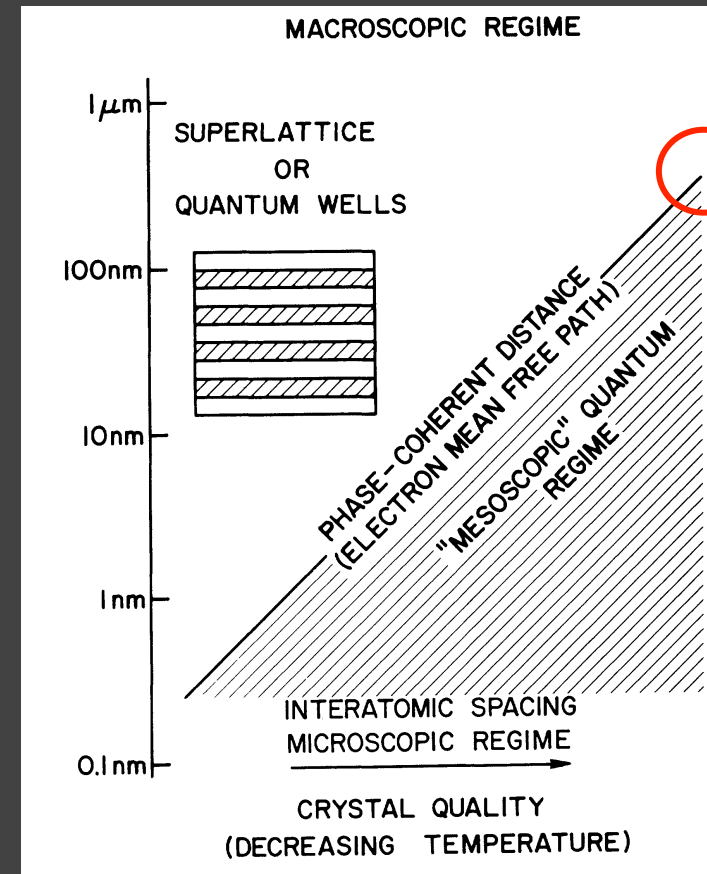
$$\lambda = \tau v$$

τ : scattering time

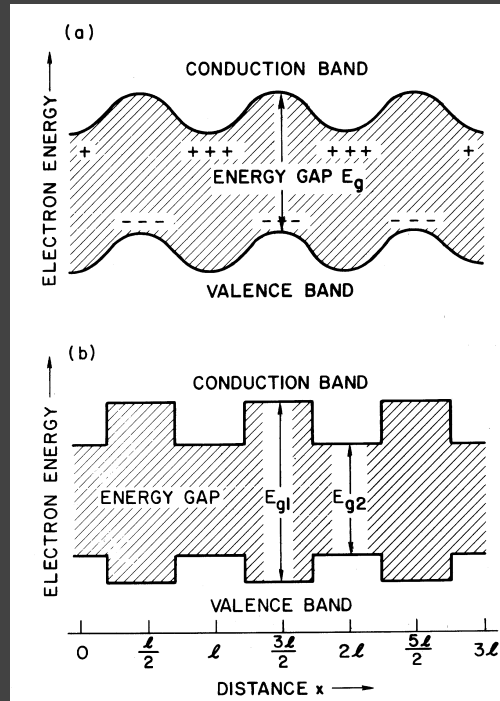
v : (thermal or Fermi) velocity

The wavefunction phase is well-defined:

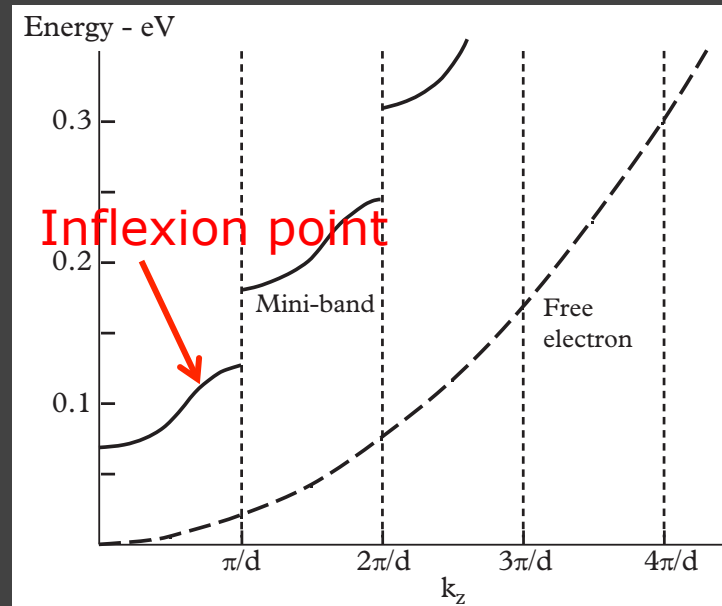
- For times shorter than τ
- For lengths shorter than λ



Electron transport in superlattices



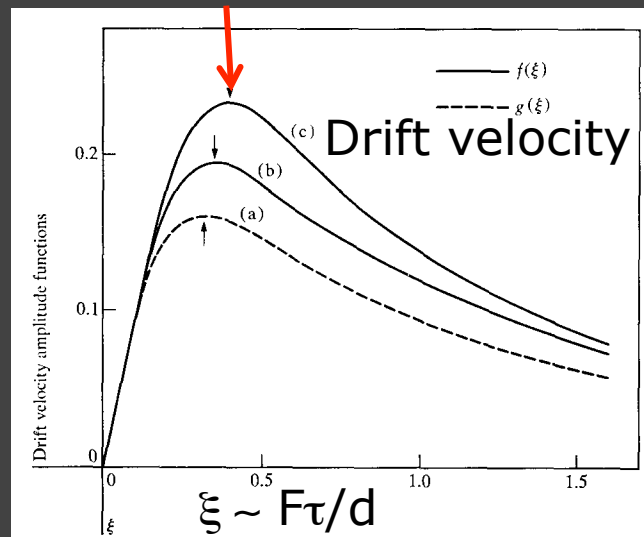
Energy dispersion



At room T
For $\mu = 2500 \text{ cm}^2/\text{Vs}$
 $\lambda \sim 50 \text{ nm}$

F electric field

$$\hbar \dot{k}_z = eF$$



Materials

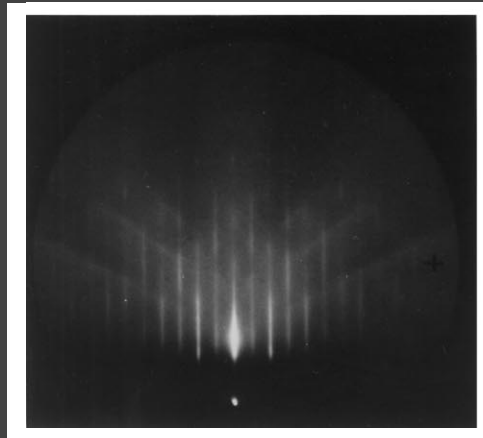
The achievement of a well-defined superlattice structure with a period of, say, 100\AA will require considerable effort even with the use of the most advanced epitaxial thin-film technologies. The materials should be well-known semi-conductors and their alloys; for examples, Ge, Si, Ge-Si alloys, III-V compounds and their alloys, II-VI com-

At that time...



Surface Physics

- Atomic adsorption studies
- HEED/LEED
- UHV
- Substrate preparation

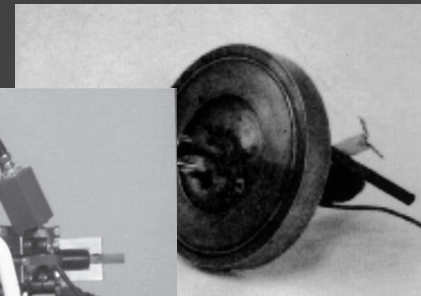


HEED GaAs substrate



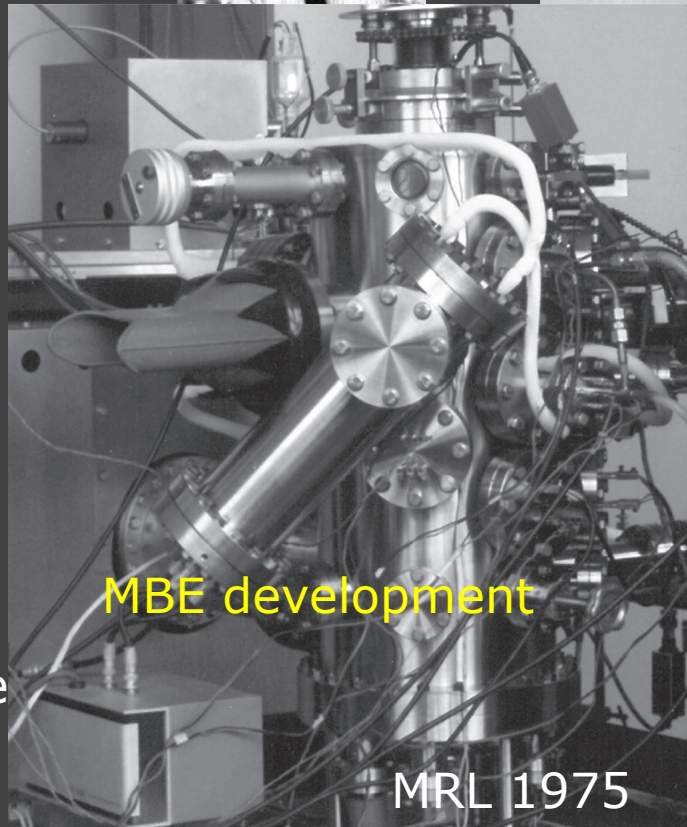
Spatial technologies

- Development of effusion cells



for experiments on ion propulsion

crosshroud
temperature controller
block



MBE development

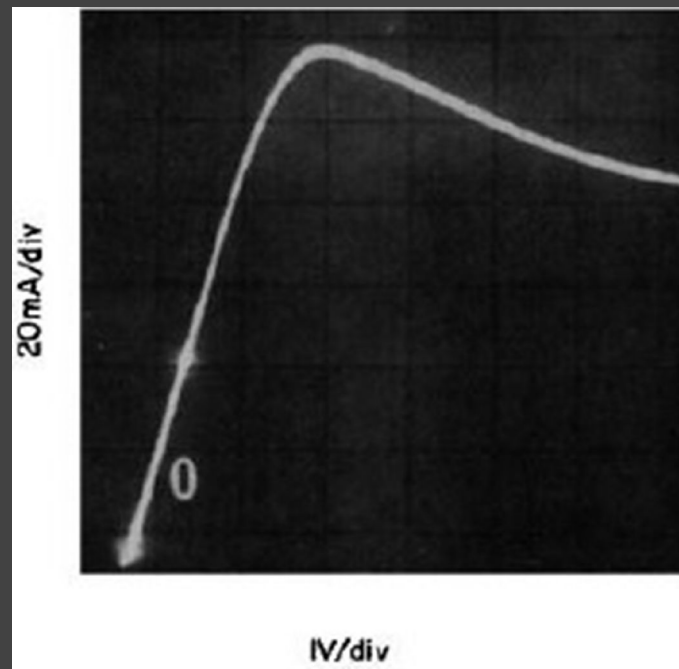
MRL 1975

1972: Esaki and Chang



Esaki and Chang built their own system at IBM

Measurement of negative resistance in AlGaAs/GaAs SL (70 Å period)

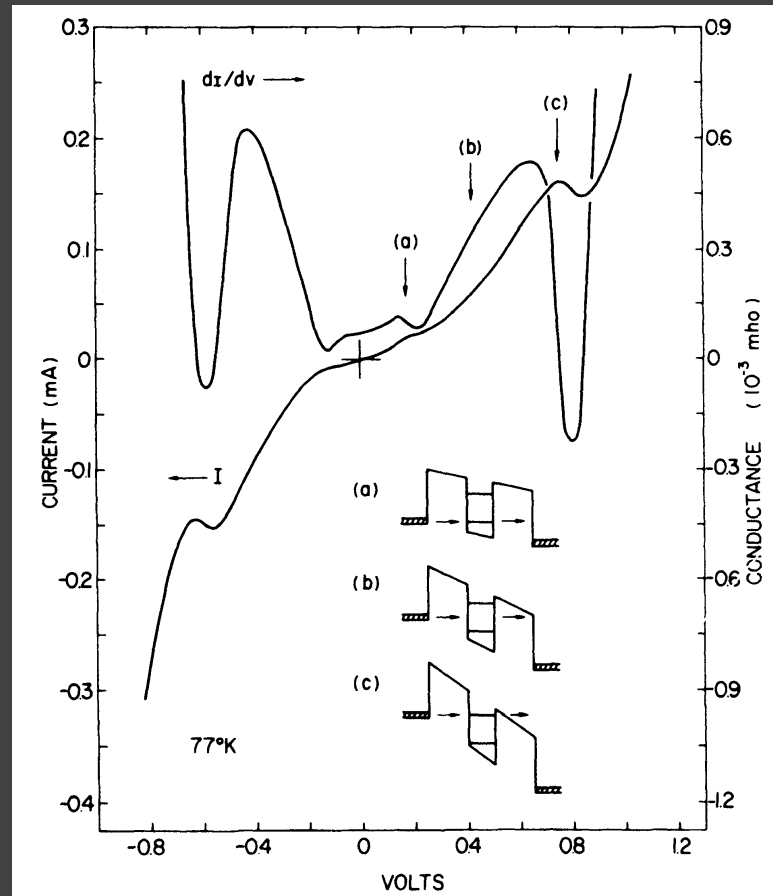


A measurable quantum effect !

1974 : Resonant tunneling in double-barriers



Chang, Esaki and Tsu

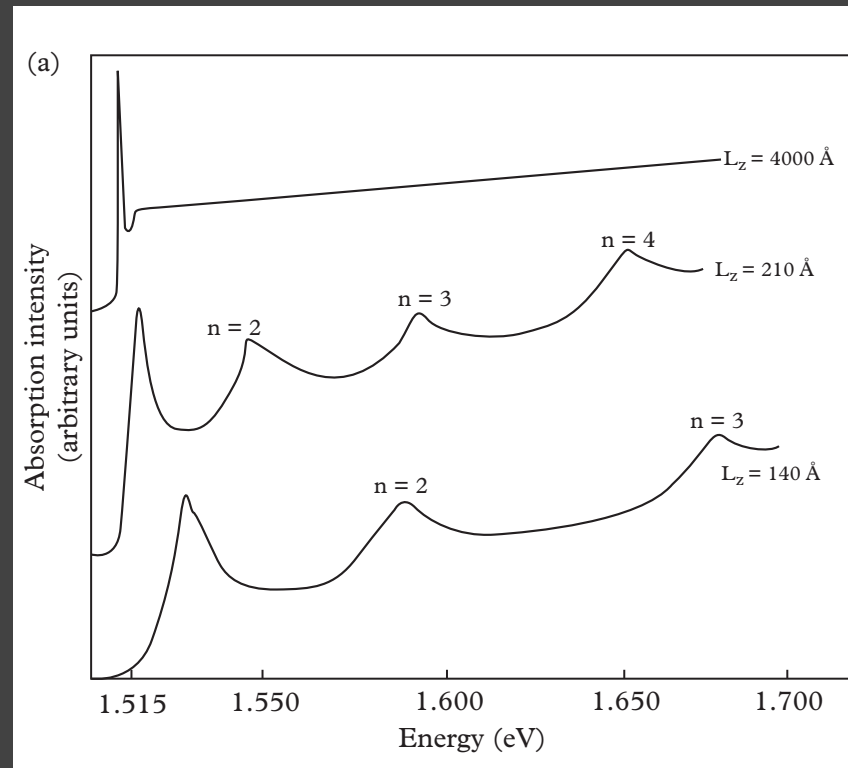


1974 Optical properties of QWs



At Bell Labs

Absorption AlGaAs/GaAs QW



Dingle et al. PRL

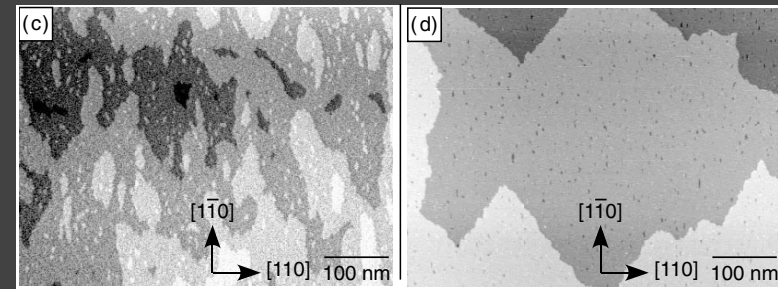
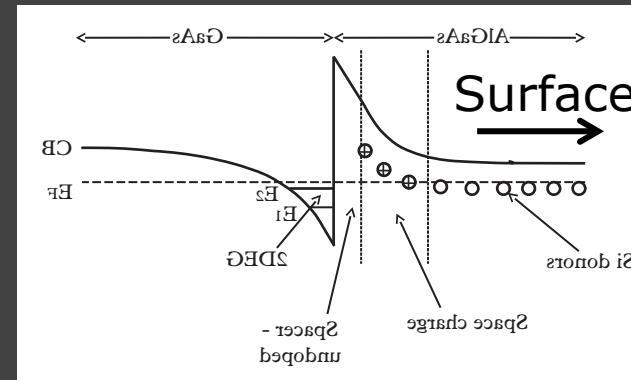
Direct visualization of quantum effect due to confinement

2D electron gas

In 1978, $\mu \sim 10^4 \text{ cm}^2/\text{V.s}$

A long series of improvement

- High purity sources
- Remote doping (1981)
spacer layer thickness
- Inverted interface (1981)
- Short GaAs/AlAs SL ("super réseau poubelle") (1984)
- Planar doping (1980)
- Double planar doping (1987)
- Temperature and As pressure control (1985)



3x1 RHEED surface reconstruction

Obtained for As/Ga ratio close to 1

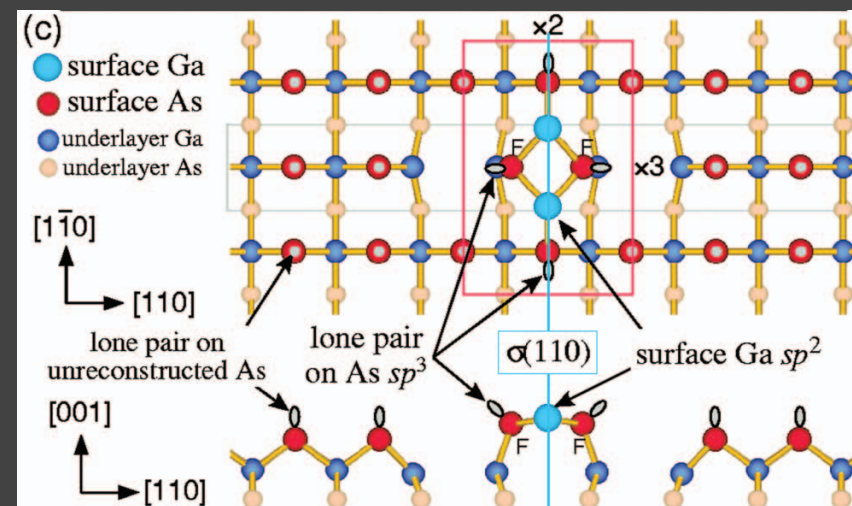
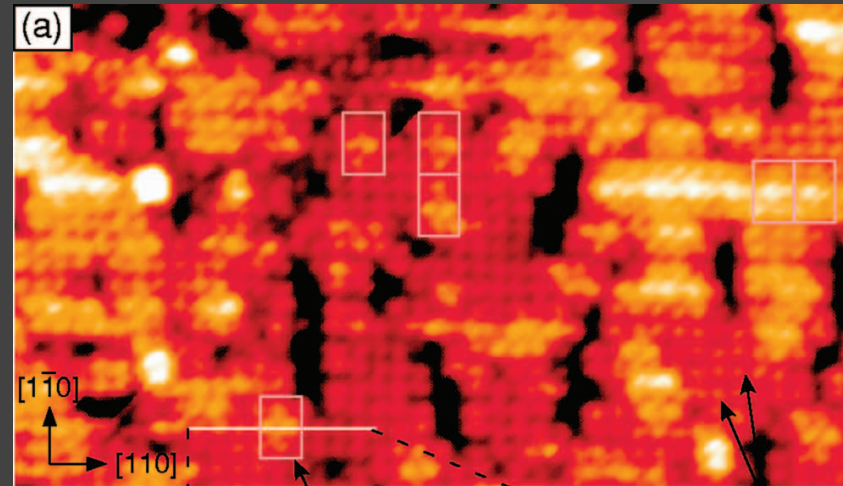


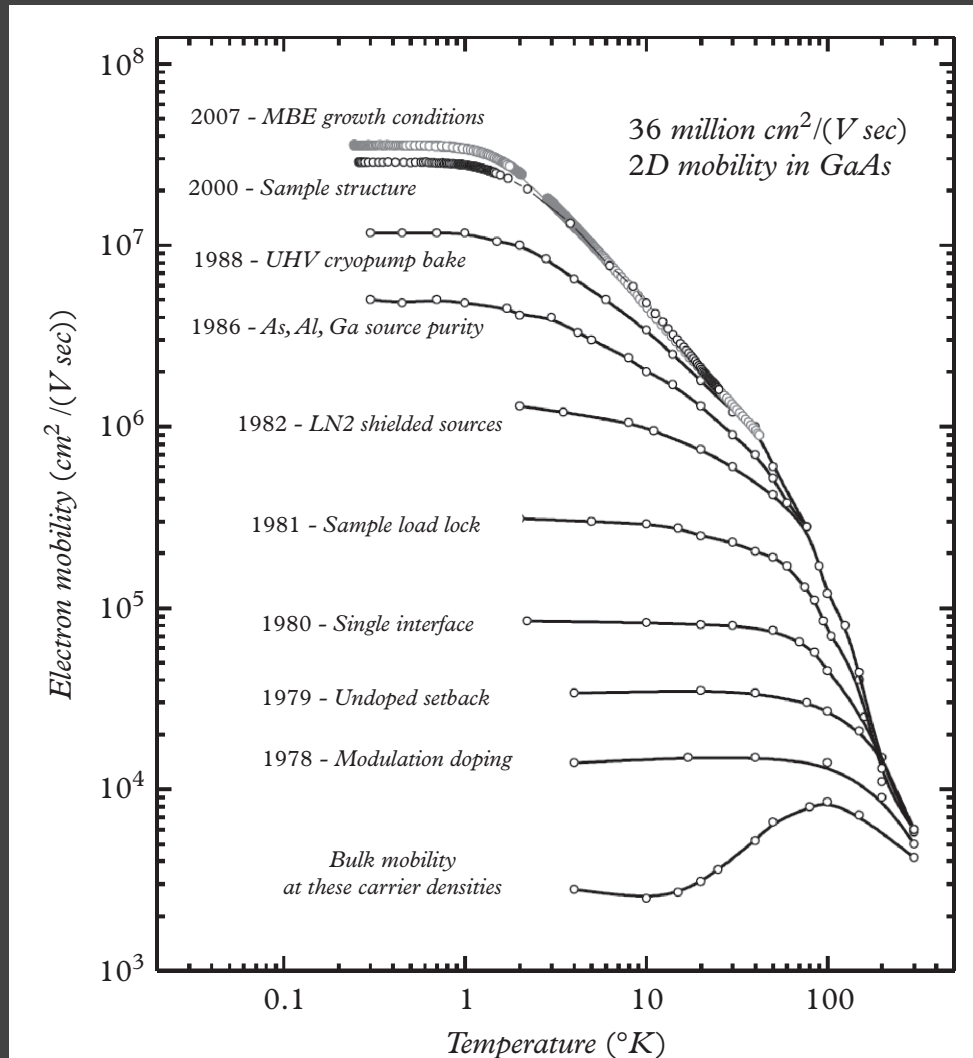
Martrou PRB 2005

Mixed surface:
(1x1) cells 45%
(3x2) cells 39%
others

27% decrease of the sp^2 reactive Ga sites compared to $\beta_2(2 \times 4)$

Less impurity incorporation





$10^7 \text{ m}^2/\text{V.s}$



(Mobility) mean free path
 $\lambda \sim 150 \mu\text{m}$!

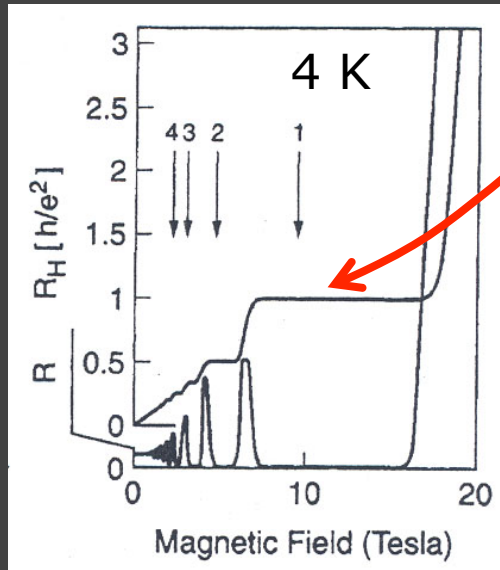
Mesoscopic experiments

- in-plane transport
- over very large distances

Schlom and Pfeiffer 2010

The fractional quantum Hall effect

Integer quantum Hall effect: a single particle effect



Hall plateaus

- Quantized resistance $R_H = h/e^2 \sim 25k\Omega$
- Landau levels
- Edge modes
- involve impurities

The one that "only provided the sample"

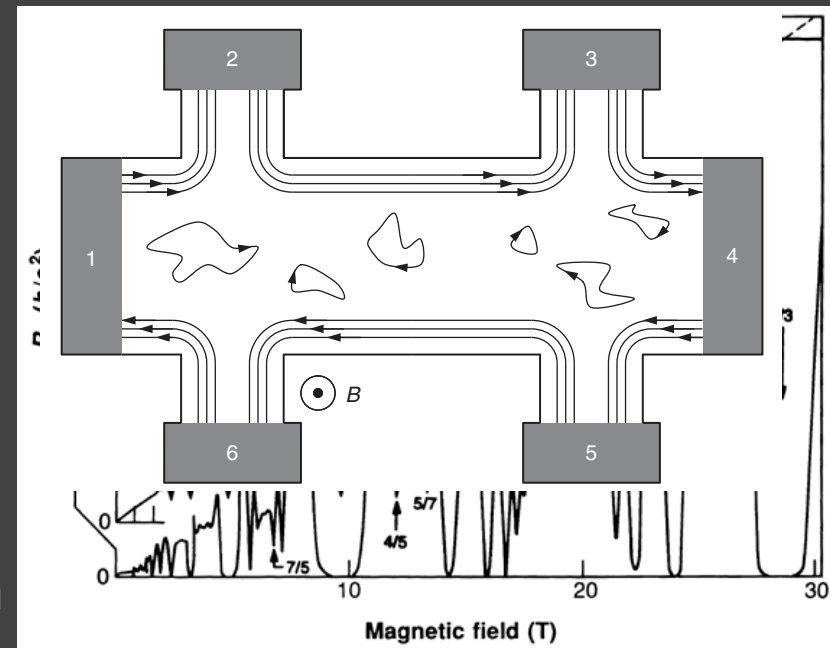
Störmer, Tsui, Gossard (1982)
AlGaAs/GaAs high mobility 2DEG

Klitzing et al (1980)
Si/SiO₂ MOSFET
(rough interface)

FQHE : a collective effect

New composite particles with fractional charge: $e/3, e/5, e/7...$

1 electron + 2, 3,... magnetic flux quanta





Mesoscopic transport

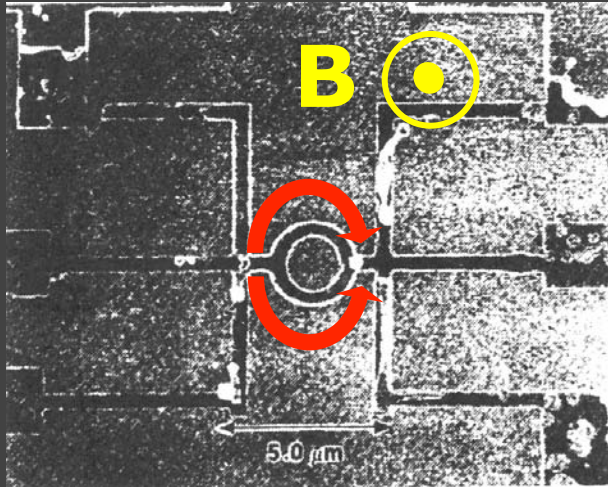
Aharonov-Bohm effect

Mankiewich et al. (88)



Interference effect

Phase difference between the two paths



AlGaAs/GaAs ring

B induces a magnetic flux Φ through the loop.

Electrons pick up a phase

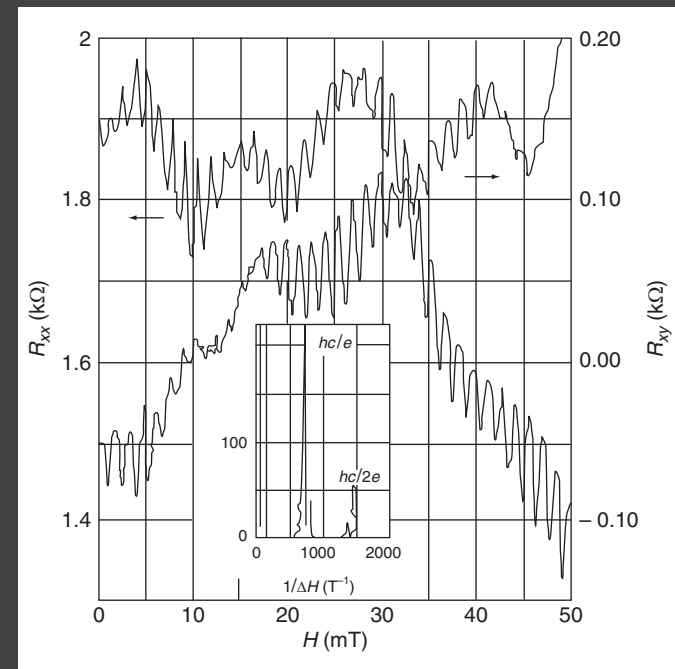
$$\varphi = \varphi_0 + \frac{1}{\hbar} (\mathbf{p} + e\mathbf{A}) \cdot \mathbf{r},$$

A: potential vector

$$\delta\varphi = \frac{e}{\hbar} \int_0^{2\pi} \mathbf{A} \cdot \mathbf{a}_\vartheta r d\vartheta = \frac{e}{\hbar} \int_{ring} \mathbf{B} \cdot \mathbf{n} dS = 2\pi \frac{\Phi}{\Phi_0},$$

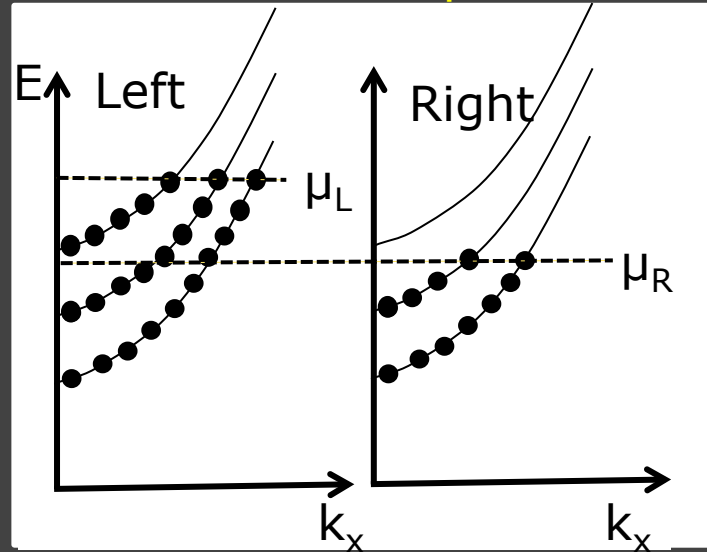
$$\Phi_0 = h/e$$
 Quantum flux

Magneto-resistance oscillations



Quantum point contact

Ballistic transport in 1D



Thomas et al. PRL 96

Constriction

1D modes (or channels)

$$E_n = \left[n + \frac{1}{2} \right] \hbar \omega_0 + \frac{\hbar^2 k_x^2}{2m^*}, \quad n = 1, 2, 3, \dots$$

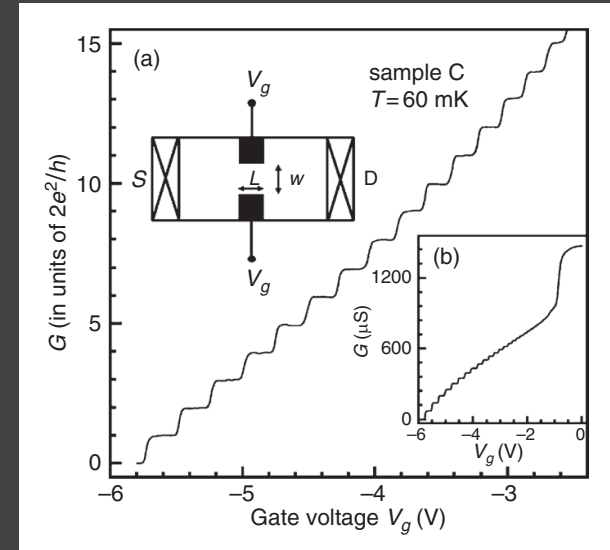
1D State density

$$D_n(E) = \frac{2}{\pi} \frac{\partial k_x}{\partial E}$$

Group velocity

$$v_n(E) = \frac{1}{\hbar} \frac{\partial E}{\partial k_x}$$

Van Wees et al. 1988
Wharam et al. 1988



For a perfect conductor (T=1)

$$\begin{aligned} I &= e \times \sum_{n \text{ occ } \mu_D}^{\mu_S} \int v_n(E) D_n(E) dE \\ &= e \times \sum_{n \text{ occ}} \frac{2}{h} \int_{\mu_D}^{\mu_S} dE \\ &= e \times n \times \frac{2}{h} \times eV \end{aligned}$$

At T=0K

$$G = n \frac{2e^2}{h} \approx n \times \frac{2}{25.8 \text{ k}\Omega}$$



Light-matter interaction in semiconductor heterostructures

The dielectric constant of semiconductors



$$\mathbf{D} = \varepsilon_0 \mathbf{E} + \mathbf{P}$$

D: electric displacement field
P: polarization density or electric dipole moment per unit volume

In a linear, homogeneous, isotropic dielectric medium

$$\mathbf{P} = \varepsilon_0 \chi \mathbf{E} \quad \chi: \text{Electric susceptibility}$$

$$\mathbf{D} = \varepsilon_0 (1 + \chi) \mathbf{E} = \varepsilon_0 \varepsilon_r \mathbf{E} \quad \varepsilon_r: \text{relative permittivity or dielectric constant}$$

$$\tilde{n} = \sqrt{\varepsilon_r} \quad \text{Complex refractive index}$$

To interact with matter, light (frequency ω) has to couple to oscillators

$$\varepsilon_r(\omega) = 1 + \sum_j \frac{f_j}{\omega_{0j}^2 - \omega^2 - i\omega\gamma_j}$$

Oscillator j

f_j : oscillator strength

ω_{0j} : frequency

γ_j : damping constant

Oscillators in semiconductors that couple to e.m. field



Excitons

Optical properties close to the gap
NIR, visible, UV

Phonons

- Optical properties (optical phonon) in the IR range
- Raman (optical phonon) and Brillouin (acoustic phonon) scattering

Plasmons

In highly doped structures
in the IR range (semiconductors)

Exciton

Hydrogen-like problem

Coulomb interaction between an electron and a hole

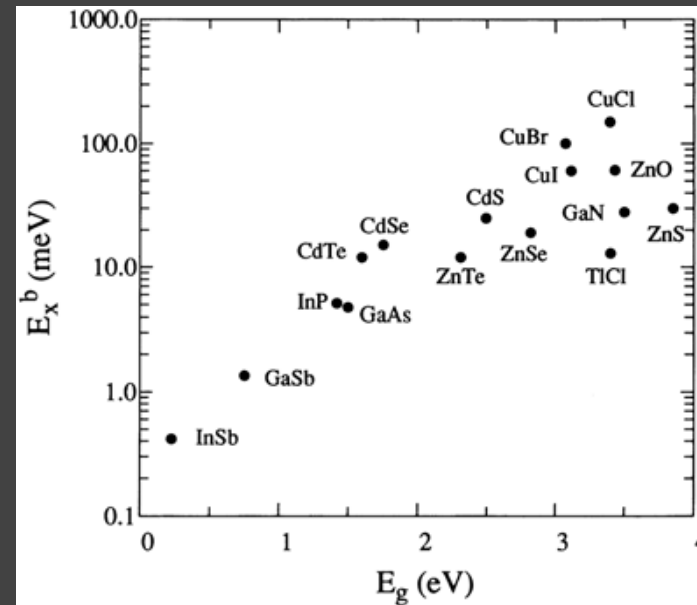
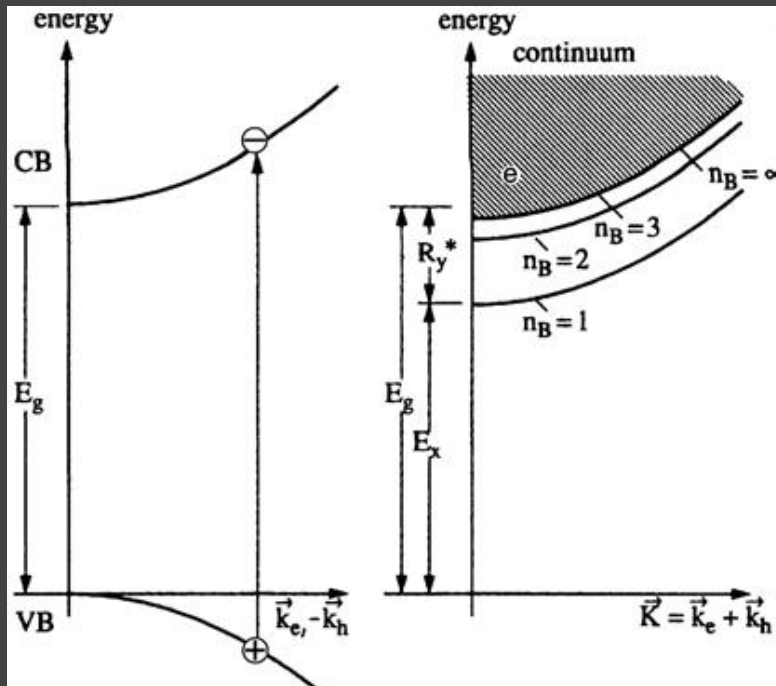
$$E_{\text{ex}}(n_B, \mathbf{K}) = E_g - Ry^* \frac{1}{n_B^2} + \frac{\hbar^2 \mathbf{K}^2}{2M}$$

Exciton translational mass and wave vector

$$M = m_e + m_h, \quad \mathbf{K} = \mathbf{k}_e + \mathbf{k}_h$$

Exciton binding energy

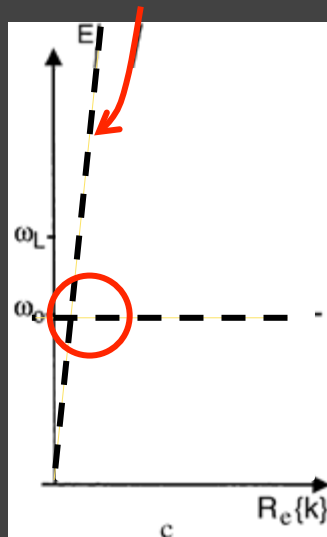
$$Ry^* = 13.6 \text{ eV} \frac{\mu}{m_0} \frac{1}{\epsilon^2} \quad \mu = \frac{m_e m_h}{m_e + m_h}$$



Polariton : mixed light matter particle

Propagating light ($\hbar\omega$, \mathbf{k}) close to an oscillator resonance (ω_0 , \mathbf{K})

Light cone



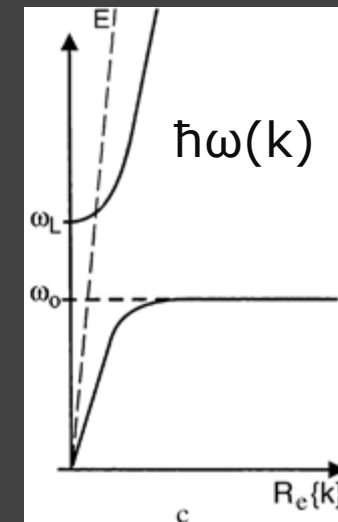
Oscillator

$$\epsilon_r(\omega) = \epsilon_b + \frac{f}{\omega_0^2 - \omega^2 - i\omega\gamma}$$

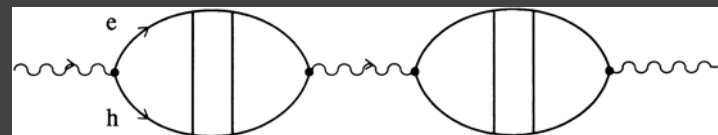
$$k^2 = [n(\omega)]^2 \left(\frac{\omega}{c}\right)^2 = \epsilon_r(\omega) \left(\frac{\omega}{c}\right)^2$$

$$\frac{c^2 k^2}{\omega^2} = \epsilon_b + \frac{f}{\omega_0^2 - \omega^2 + i\omega\gamma}$$

Polariton dispersion



Strong coupling regime: mixed photon-matter state

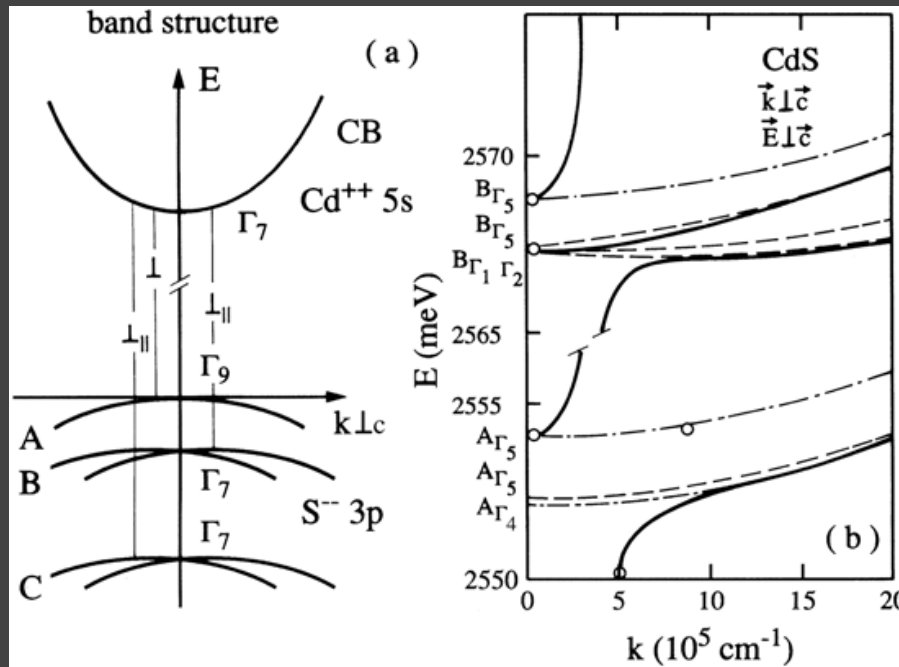


Not just an academic problem !

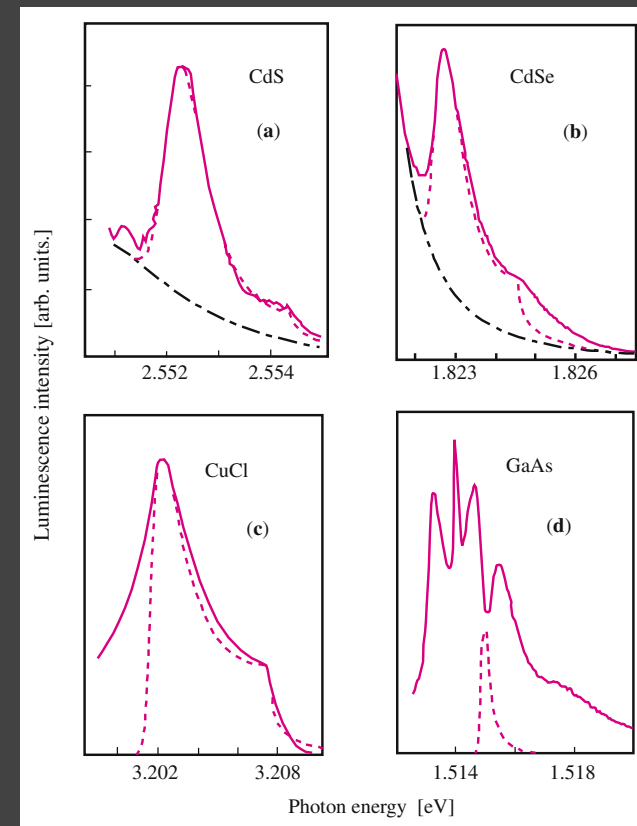
It occurs in all interaction processes between light and matter

Exciton polariton in bulk

CdS bulk
Wurzite structure
3 types of excitons



Bulk Luminescence



Nothing like a Lorentzian shape!



Polariton emission

Polariton radiative lifetime

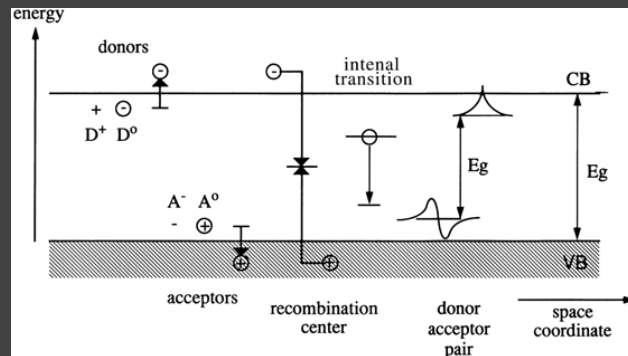
Strong coupling:

Polaritons are the system eigenstates

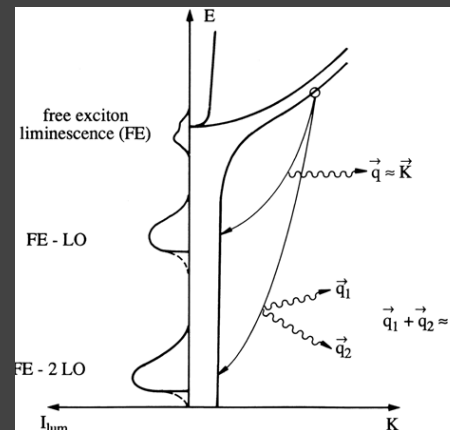
They should have an infinite radiative lifetime:
no light out!?!

Dissipative coupling or dephasing

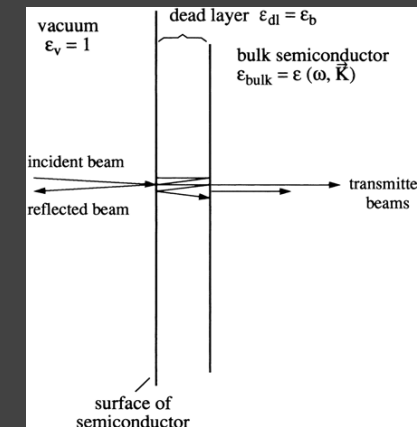
Defects



Phonons



Air/dielectric interface



In bulk long radiative lifetimes, up to several tens of ns

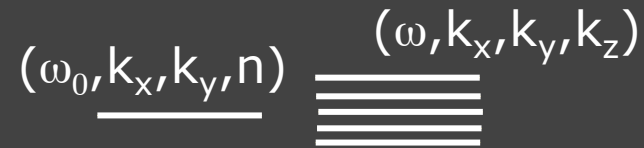
2D heterostructures like QWs



Breakdown of the polariton exciton picture

No more translational symmetry for the exciton states along z

A 2D exciton can couple to many optical modes with different k_z



Weak coupling regime

Fermi golden-rule

Decay rate

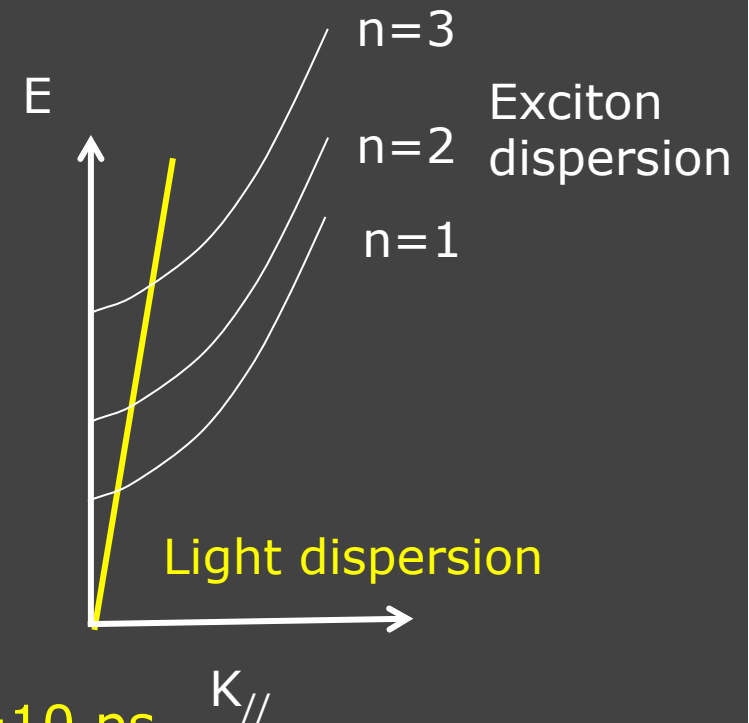
$$\Gamma_{|f\rangle \rightarrow |i\rangle} = \frac{\pi}{2\hbar} |\langle f | H_{\text{int}} | i \rangle|^2 \rho(\hbar\omega - E_i + E_f)$$

$$|i\rangle = |1 \text{ exc}, 0 \text{ ph}\rangle$$

$$|f\rangle = |0 \text{ exc}, 1 \text{ ph}\rangle$$

ρ density of optical modes

Radiative lifetime ~ 10 ps



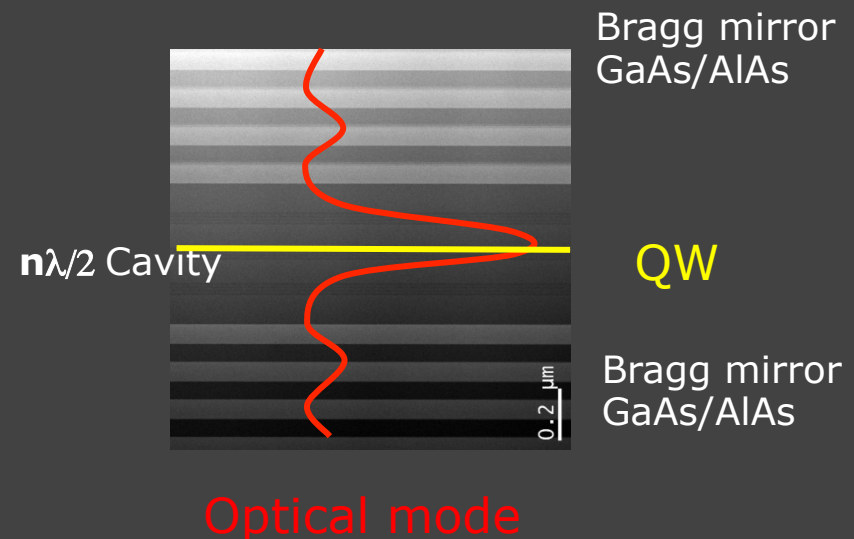
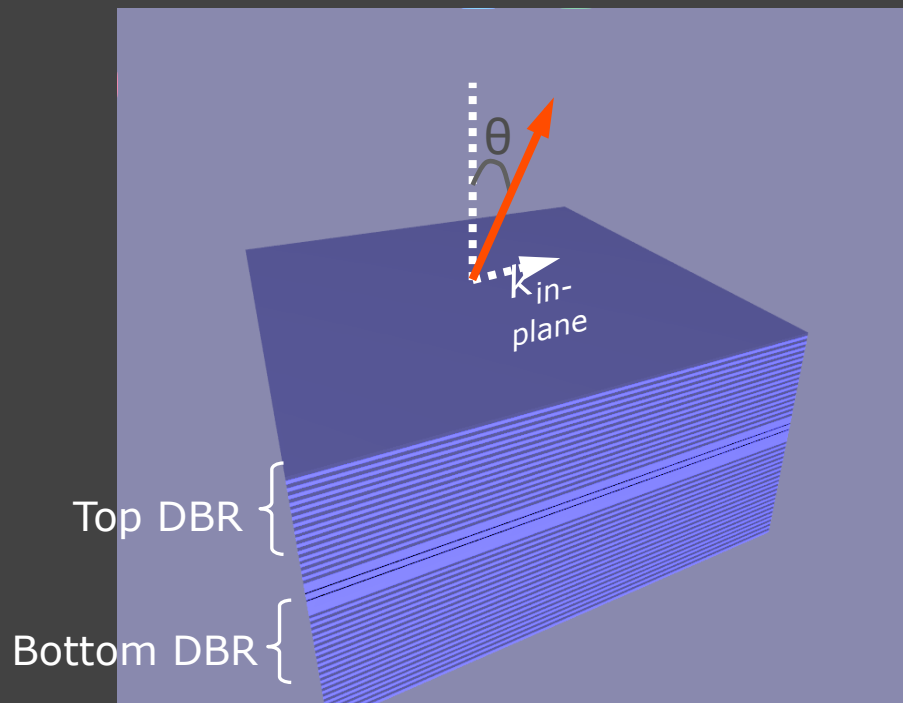
Recovering the strong coupling regime

Couple a QW exciton to a single optical mode

- discretized along z, dispersive along x and y
- localized close to the QW plane

QW inside a 2D optical cavity

GaAs $n\lambda/2$ cavity between 2 Bragg mirrors

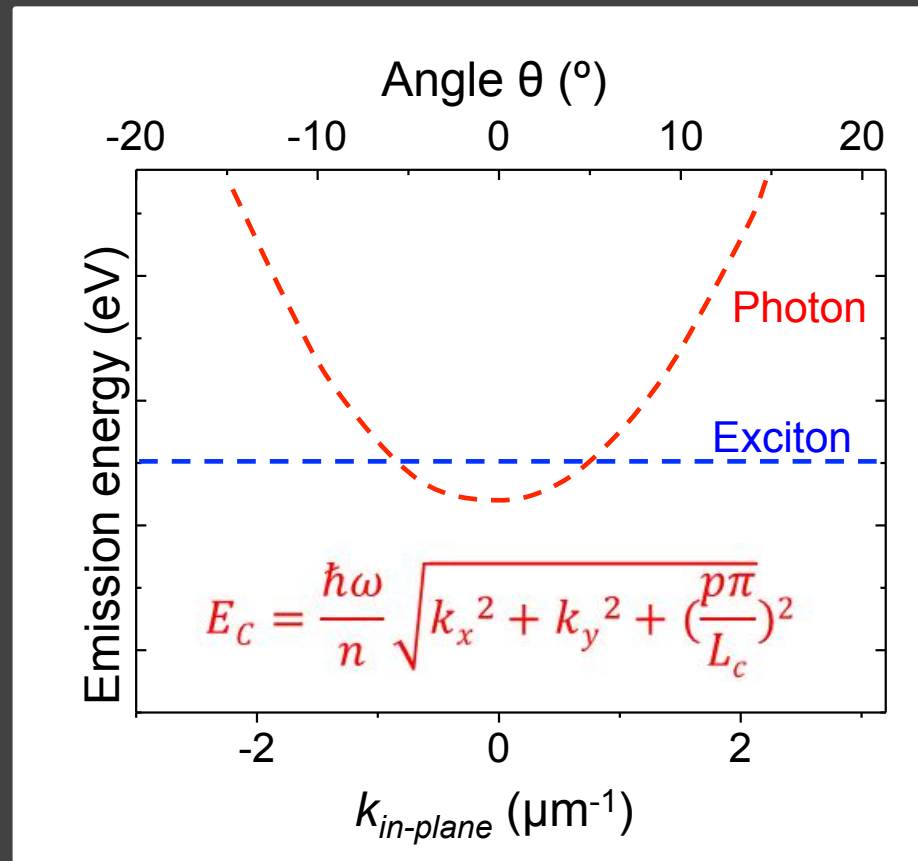


Coupling a 2D exciton to a 2D microcavity

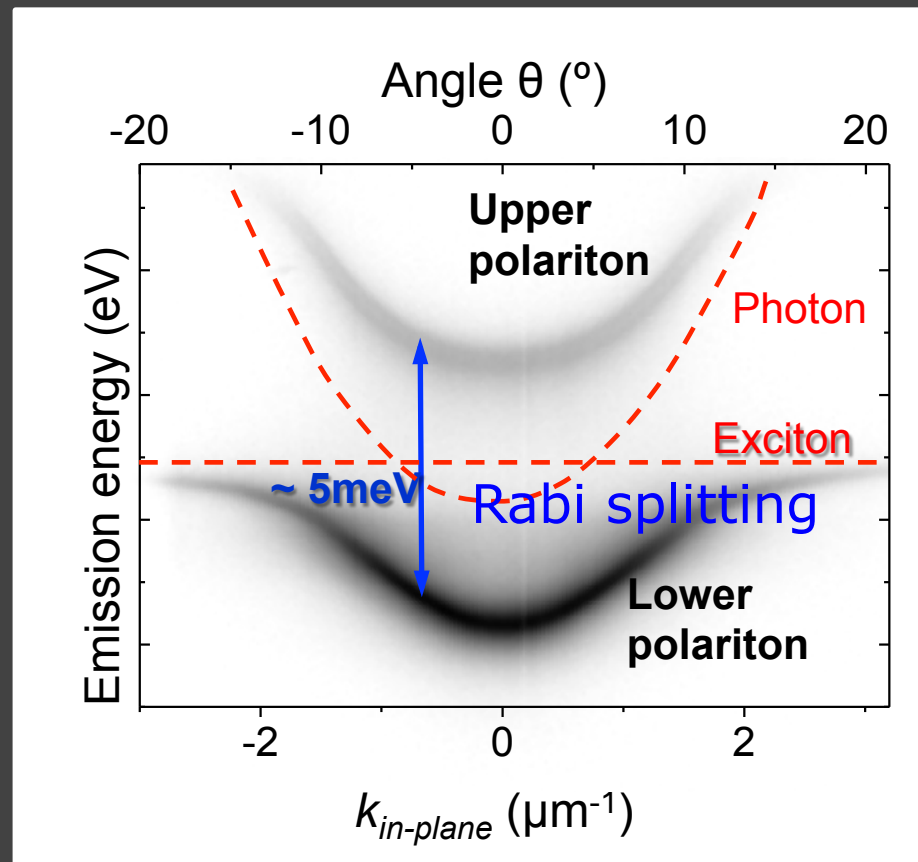


Empty cavity

A uncoupled QW exciton



Turning on the light-matter coupling



First Observation of the strong coupling



VOLUME 69, NUMBER 23

PHYSICAL REVIEW LETTERS

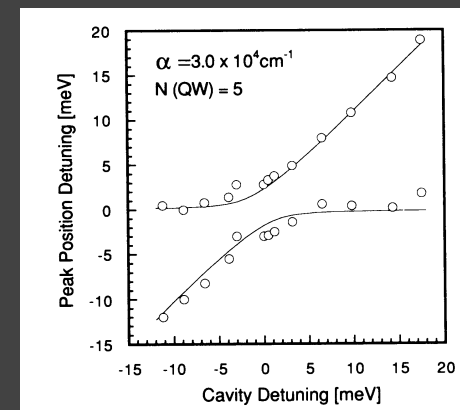
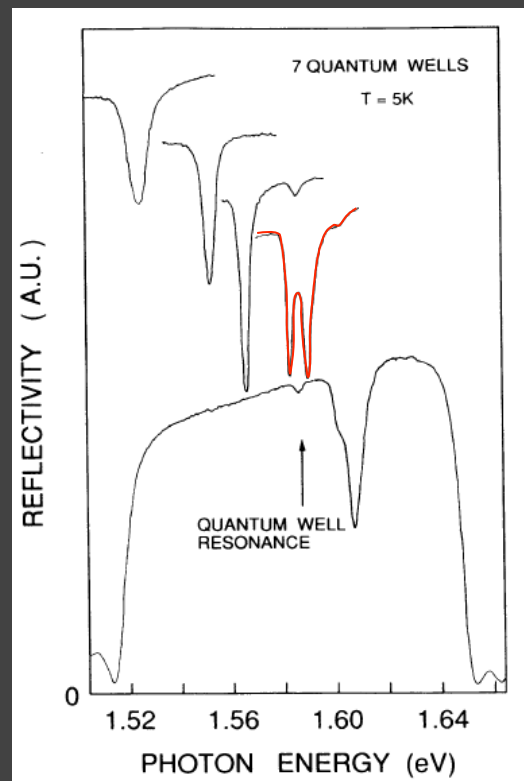
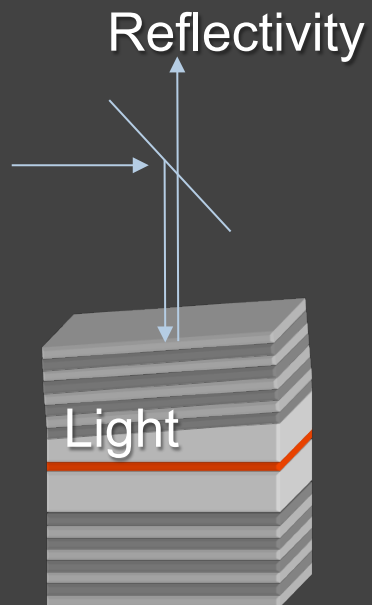
7 DECEMBER 1992

Observation of the Coupled Exciton-Photon Mode Splitting in a Semiconductor Quantum Microcavity

C. Weisbuch,^(a) M. Nishioka,^(b) A. Ishikawa, and Y. Arakawa

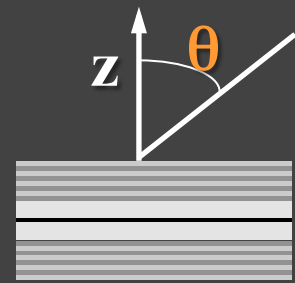
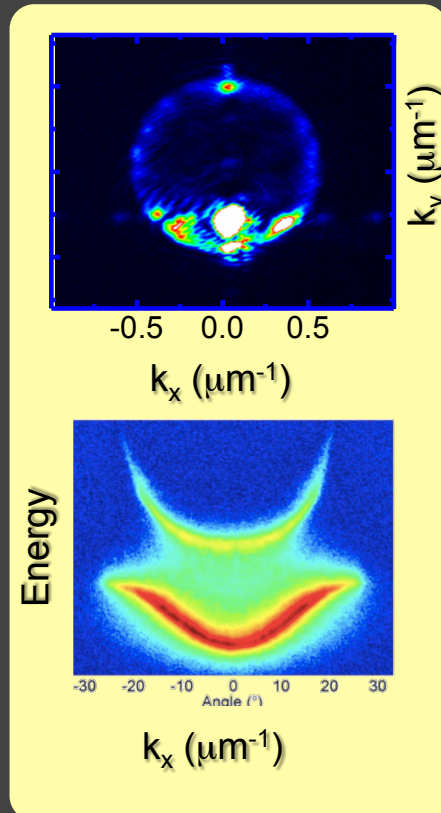
Research Center for Advanced Science and Technology, University of Tokyo, 4-6-1 Meguro-ku, Tokyo 153, Japan

(Received 12 May 1992)



Microcavity polariton emission

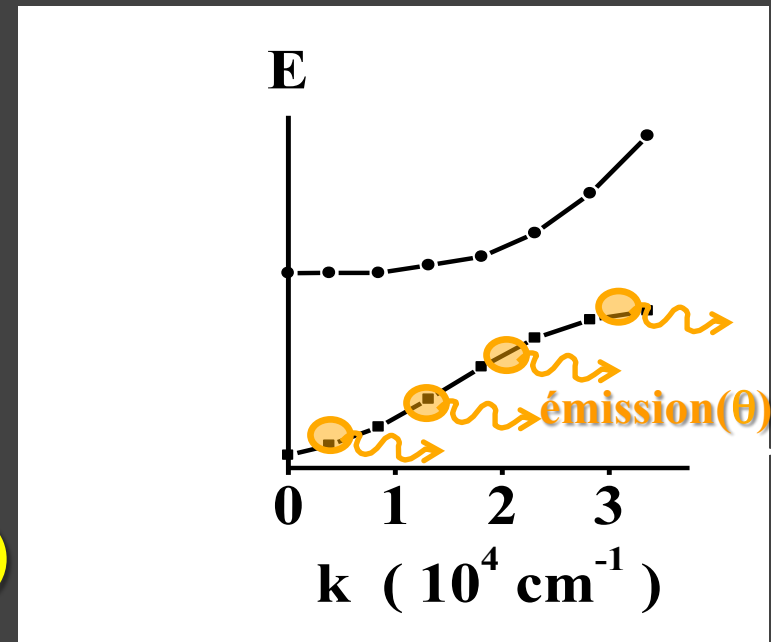
Far field pattern: Direct visualization of the polariton dispersion



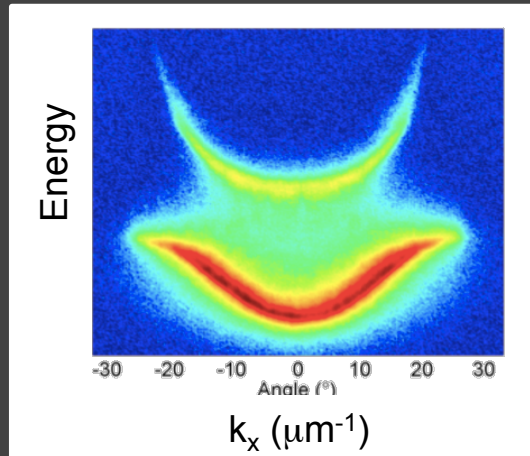
$$\theta \longleftrightarrow k_{//}$$

(d)

$$k_{//} = \omega/c \sin(\theta)$$



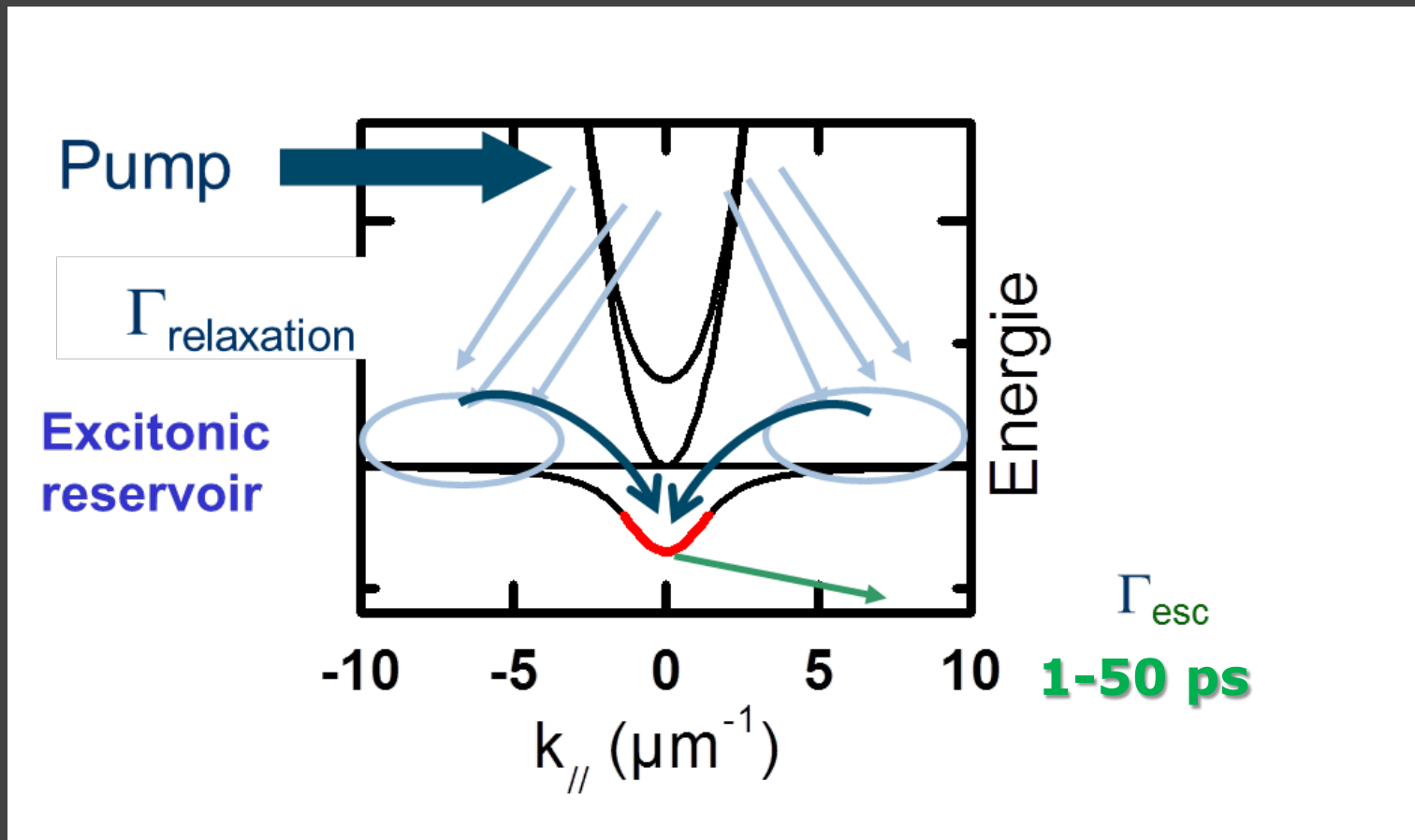
Some interesting properties



Properties

- Optical excitation and access to the polariton energy, momentum and space distribution
- Short lifetime ($\sim 1-30$ ps) \rightarrow **escape out of the cavity**
- Excitonic component \rightarrow **strong interactions**
- Photonic component \rightarrow **low mass ($10^{-5} m_e$)**
- Bosons

Polariton accumulation under non resonant condition



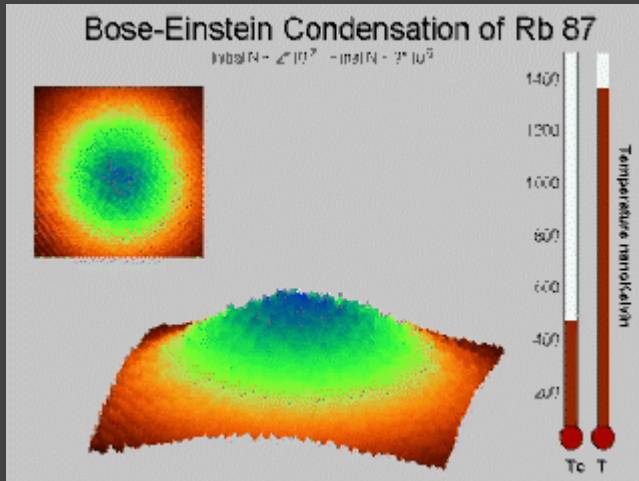
Relaxation is possible thanks to the excitonic part of the polariton

Bose Einstein Condensation in atoms



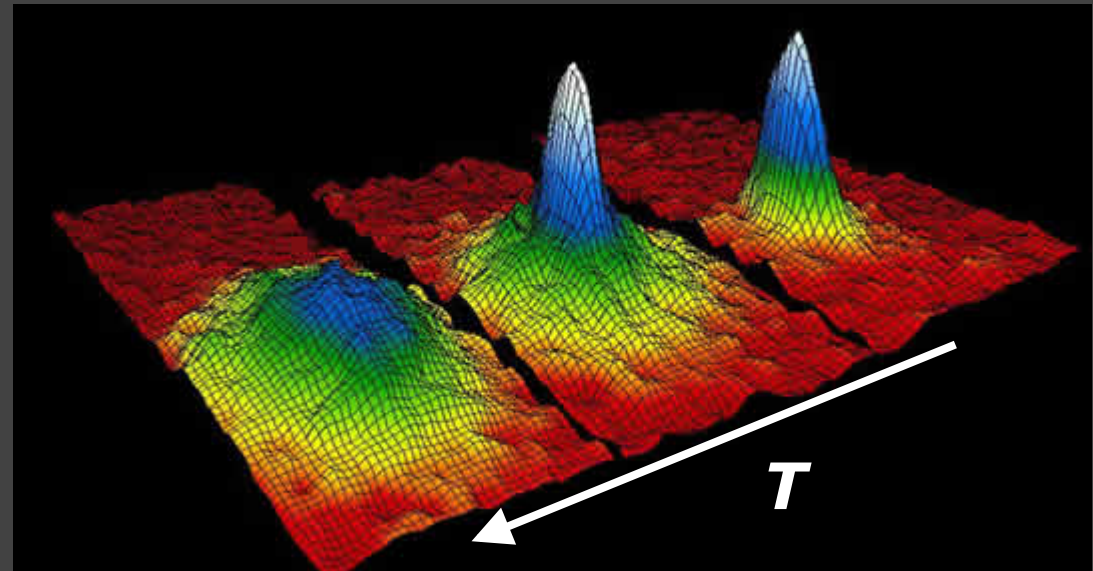
n : boson density

$$T_c = \left(\frac{n}{\zeta(3/2)} \right)^{2/3} \frac{2\pi\hbar^2}{mk_B} \approx 3.3125 \frac{\hbar^2 n^{2/3}}{mk_B}$$



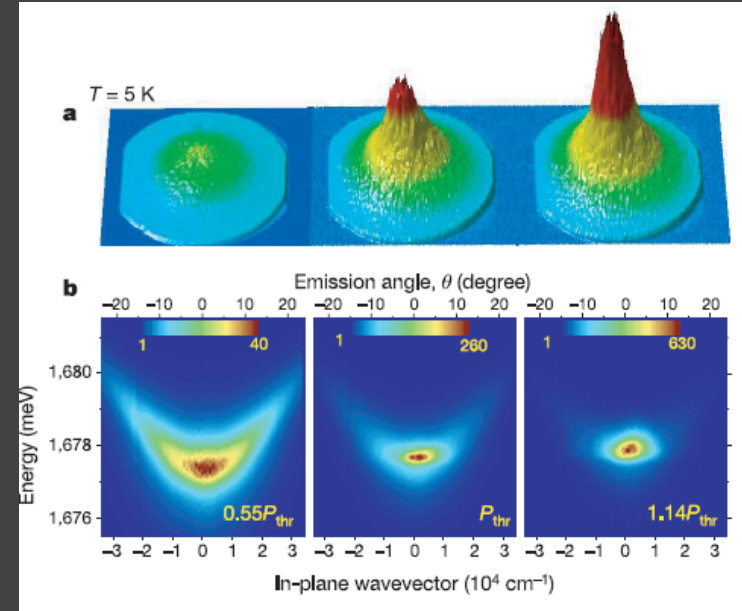
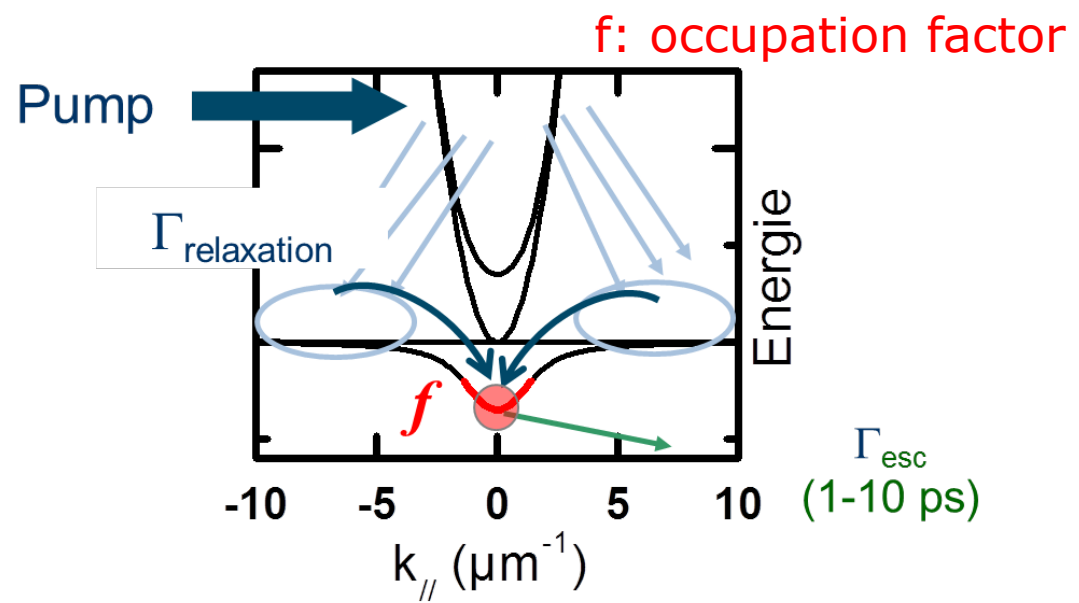
Cornell and Wieman's groups condensation of Rb atoms (1995)

- $m = 10^4 m_e$
- $T_c = 200 \text{ nK}$



<http://jilawww.colorado.edu/bec/>

Polariton condensation



Nature 443, 409 (2006)

CdTe/CdMgTe cavity

When f exceeds unity : $\Gamma_{relaxation} \propto (f+1)$ **Bosonic stimulation**

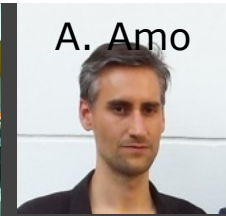
Massive occupation of the lowest energy states

Also observed in GaAs (10K), GaN, ZnO (room temperature)...

Playing with polaritons



J. Bloch



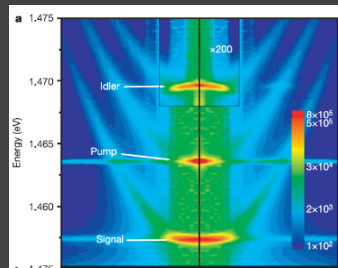
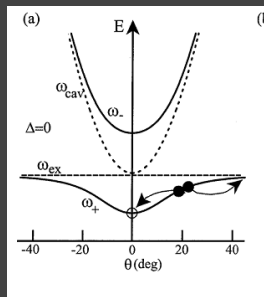
A. Amo



Polariton propagation and manipulation thanks to their photonic part polaritons have **large coherence length**

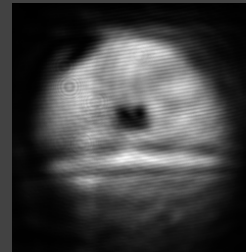
thanks to their excitonic part, polaritons **interact**

Optical Parametric Oscillator/Amplifier



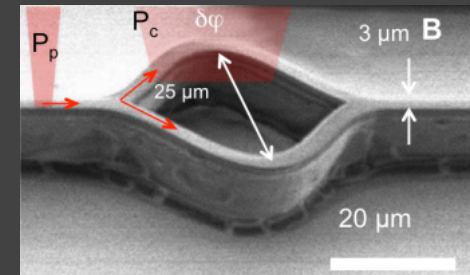
- R. Stevenson, *et al*, PRL **85**, 3680 (2000)
- P. Savidis, *et al*, PRL **84**, 1547 (2000)
- C. Diederichs, *et al*, Nature **440**, 904 (2006)

Superfluidity



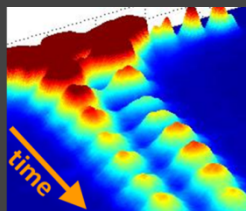
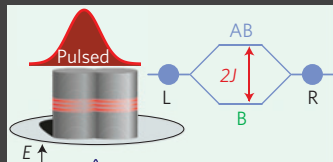
AA, Lefrère *et al.*, Nature Phys. **5**, 805 (2009)

Polariton interferometer



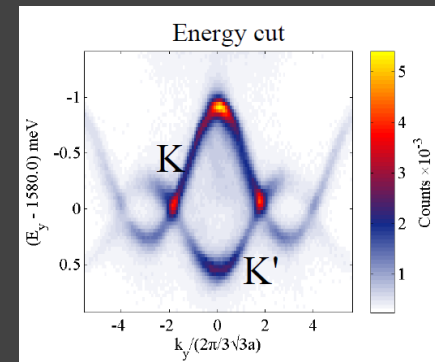
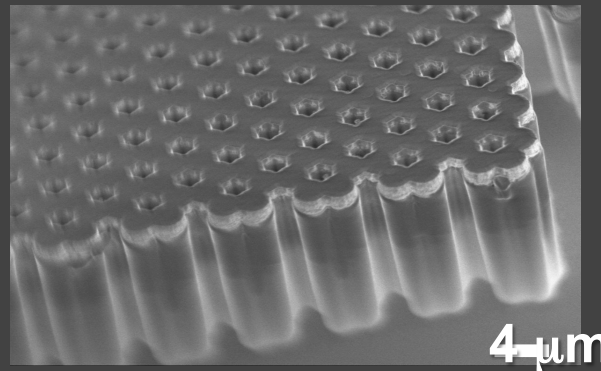
C. Sturm, *et al.*, Nat. Comm **5**, 3278 (2014)

Polaritonic molecules



M. Abbarchi *et al*

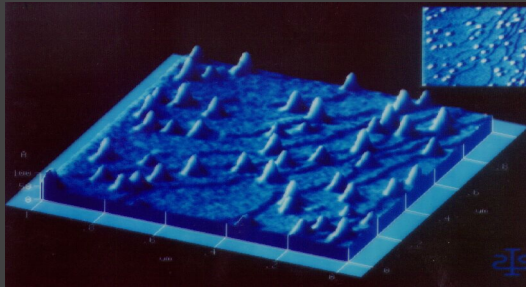
Polaritonic honeycomb lattice



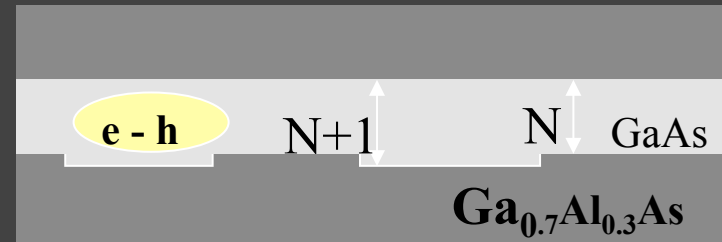
Light-matter interaction with 0D objects



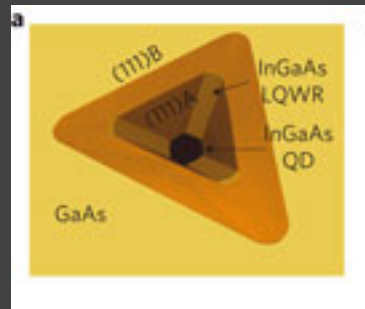
Light emission from single epitaxial emitters



Self-assembled QDs
(Stransky-Krastanov, droplets)

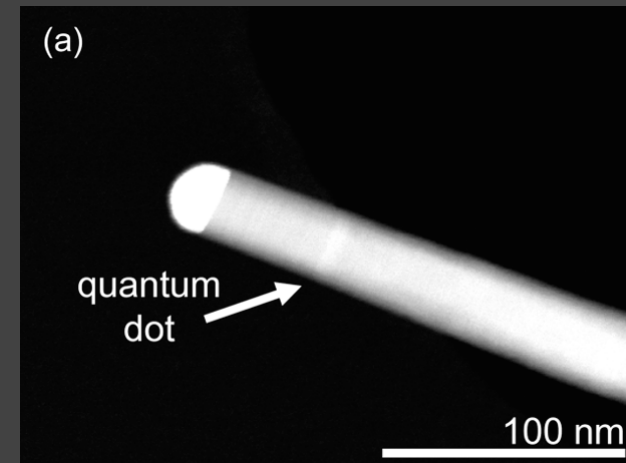


Interface fluctuations



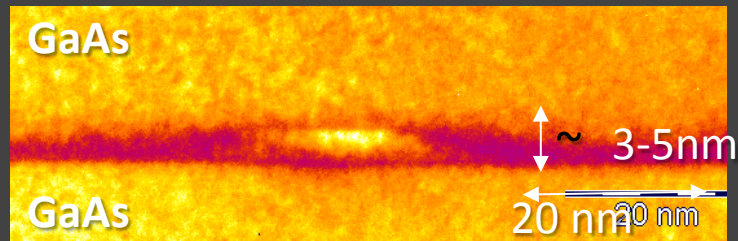
Kapon's group

Localized growth

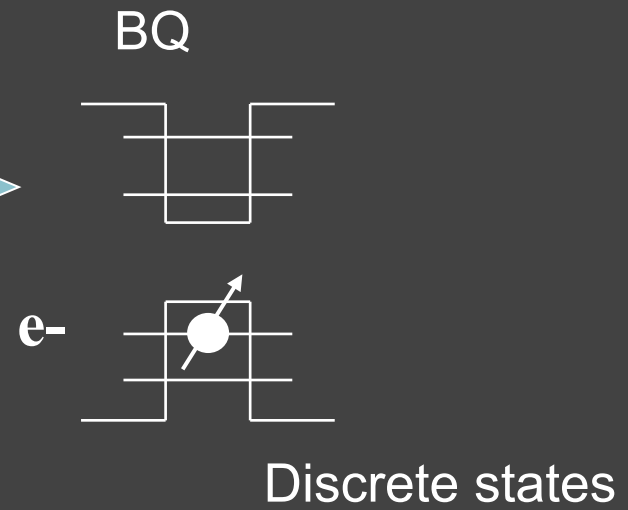


Dot in a nanowire

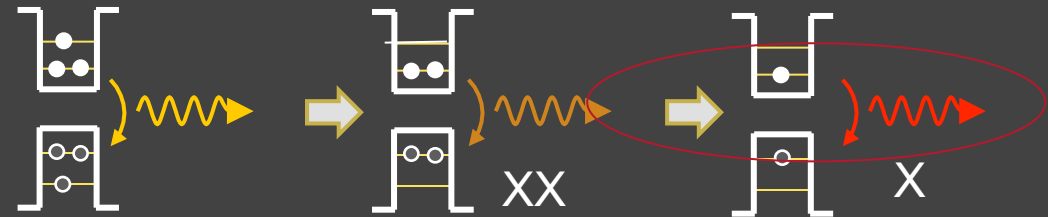
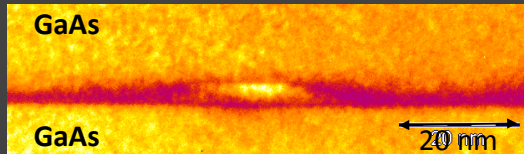
Artificial atoms



InAs/GaAs quantum dot

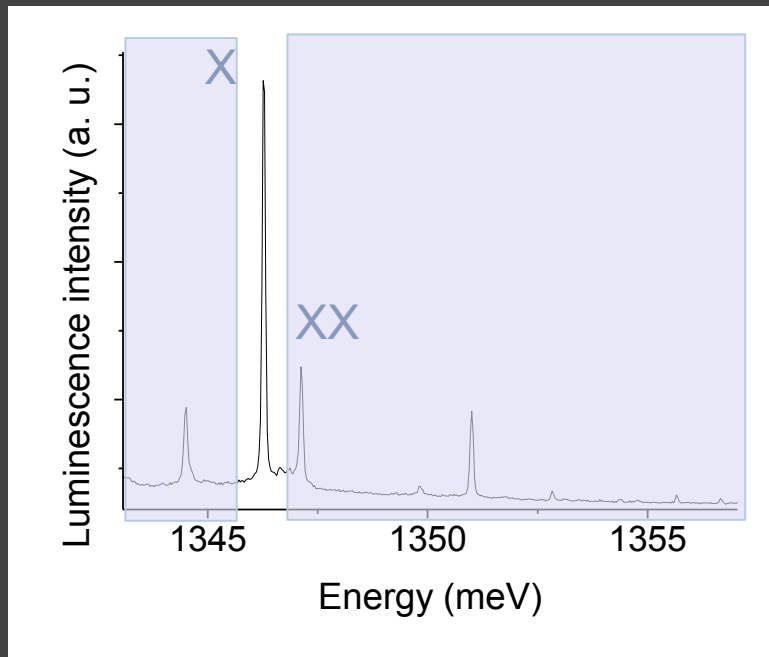


Solid state source of quantum light



biexciton

exciton

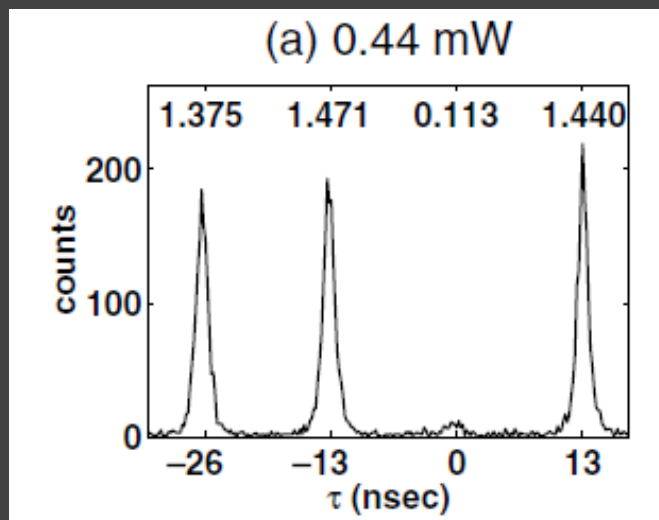


Creation of carriers in the QD (laser, bias)
Poisson statistic



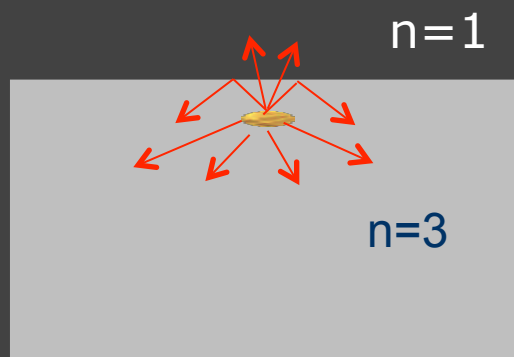
Single photon emitted at the X energy
Generation of a single photon state

Michler et al, Science 290, 2282 (2000)



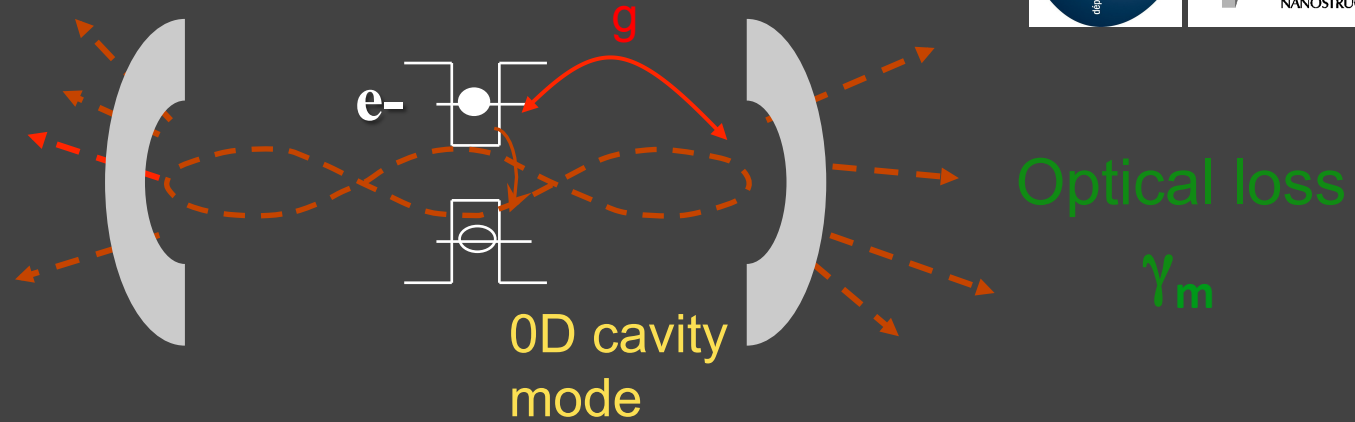
Santori et al, PRL 2001

Great source of single photons



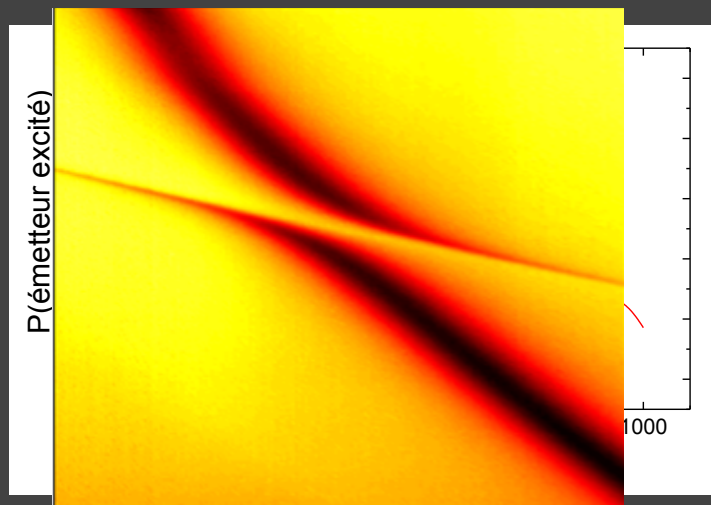
However limited extraction efficiency 3%

Coupling to a 0D cavity mode

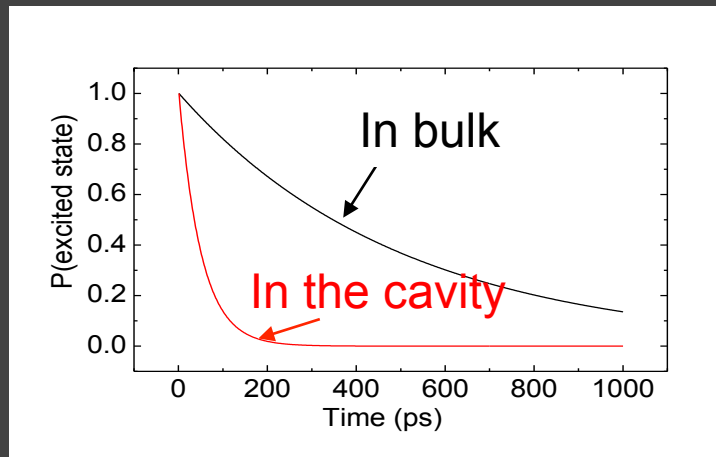


$$g \gg \gamma_m$$

$$g \ll \gamma_m$$

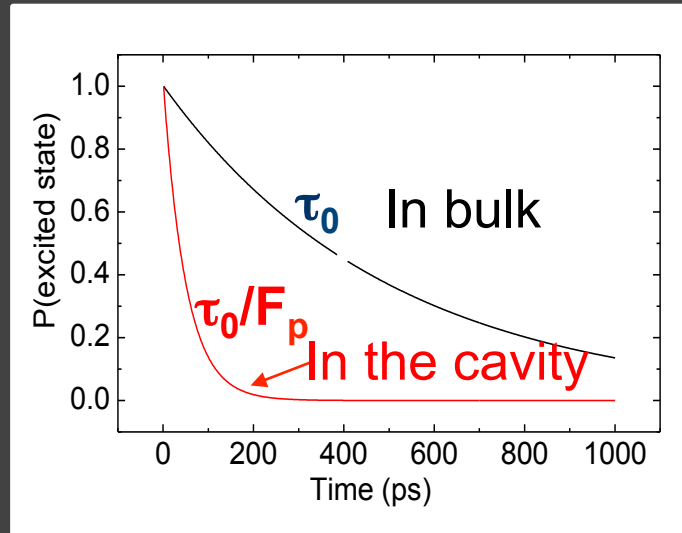


Strong coupling regime
Light-matter entangled states



Weak coupling regime
Enhanced spontaneous emission
Purcell Effect

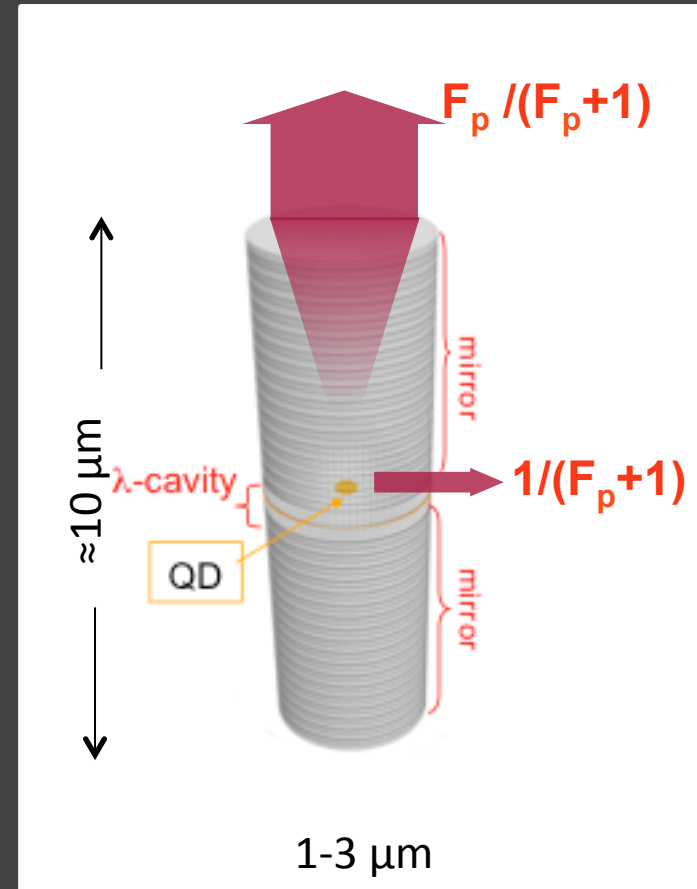
Weak coupling regime : the Purcell effect



Gérard et al, PRL 1998, Gayral et Gérard, Journal of Light. Tech. 2000

$$F_P = \frac{3}{4\pi^2} \frac{Q}{V / (\lambda_0 / n)^3}$$

Q: cavity quality factor
V: modal volume

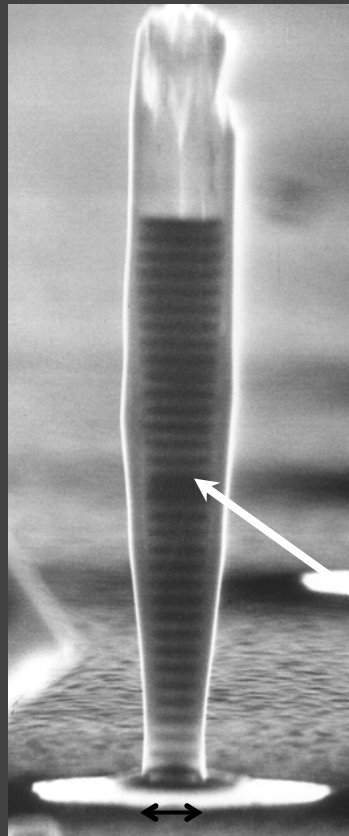


80% of emission coupled to the mode for $F_p=4$

Efficient and fast photon collection !

First demonstrations

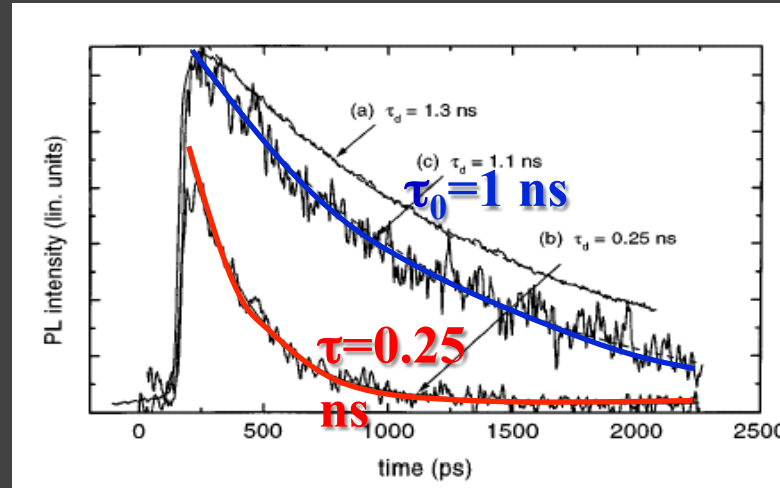
Large ensemble of QDs



1 μm

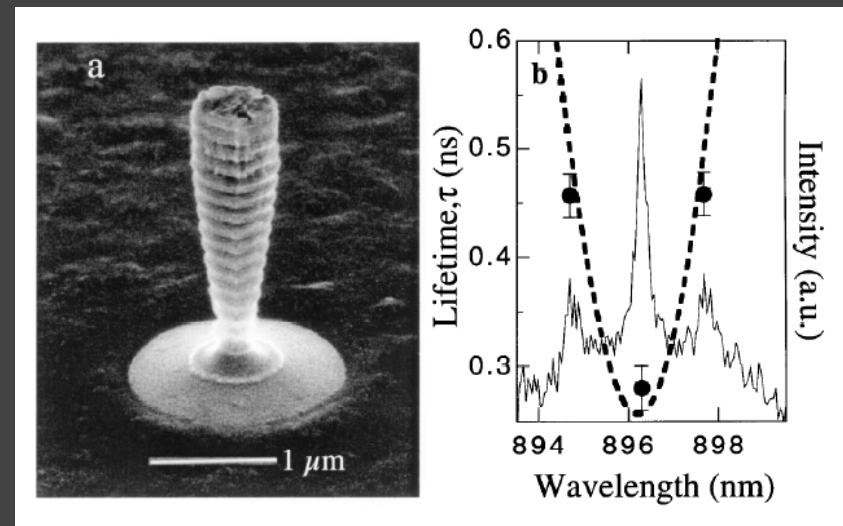
Many InAs QDs

AlAs/GaAs Micropillar:
0D optical confinement



Gérard et al (1998)

Single QD



G. Solomon et al , PRL 2000

Maximizing the Purcell effect

Spatial
matching :

&

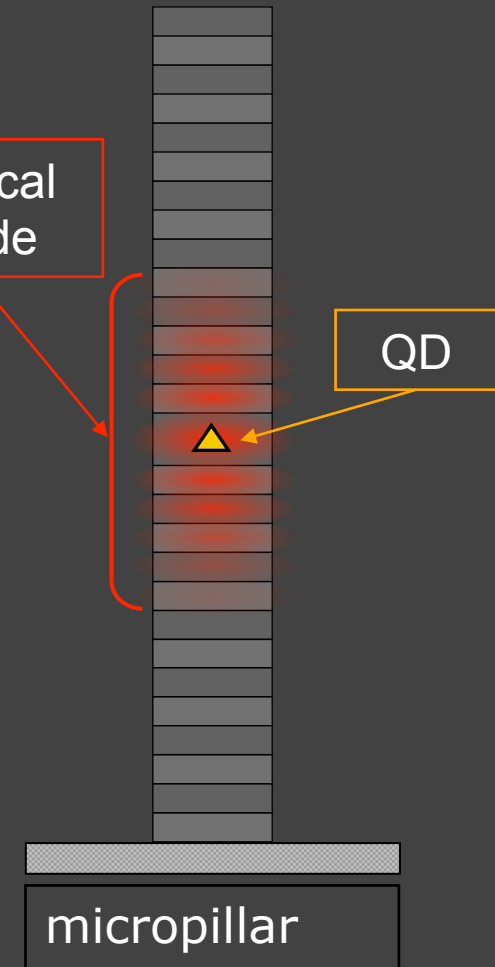
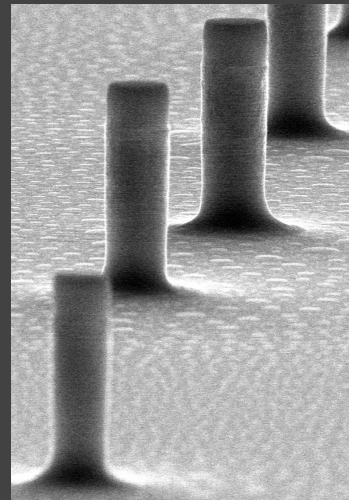
Spectral
matching :

QD at the maximum of
the field intensity

$$E_X = E \text{ mode}$$

optical
mode

QD



micropillar

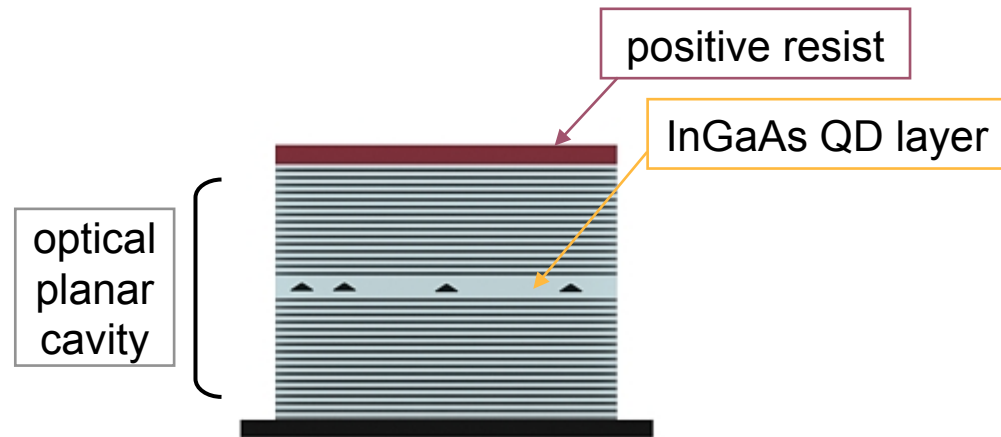
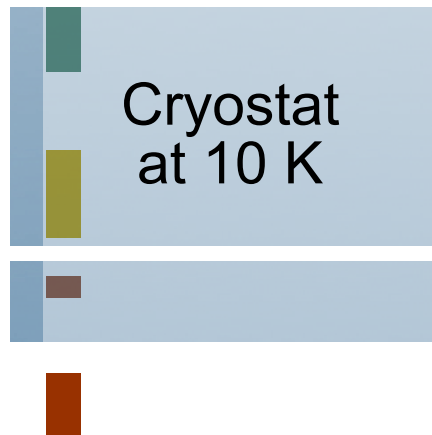
Pascale Senellart's group at LPN



An all optical technique : Low temperature in-situ lithography

- *Single step spectral and spatial matching*
- *Scalability*

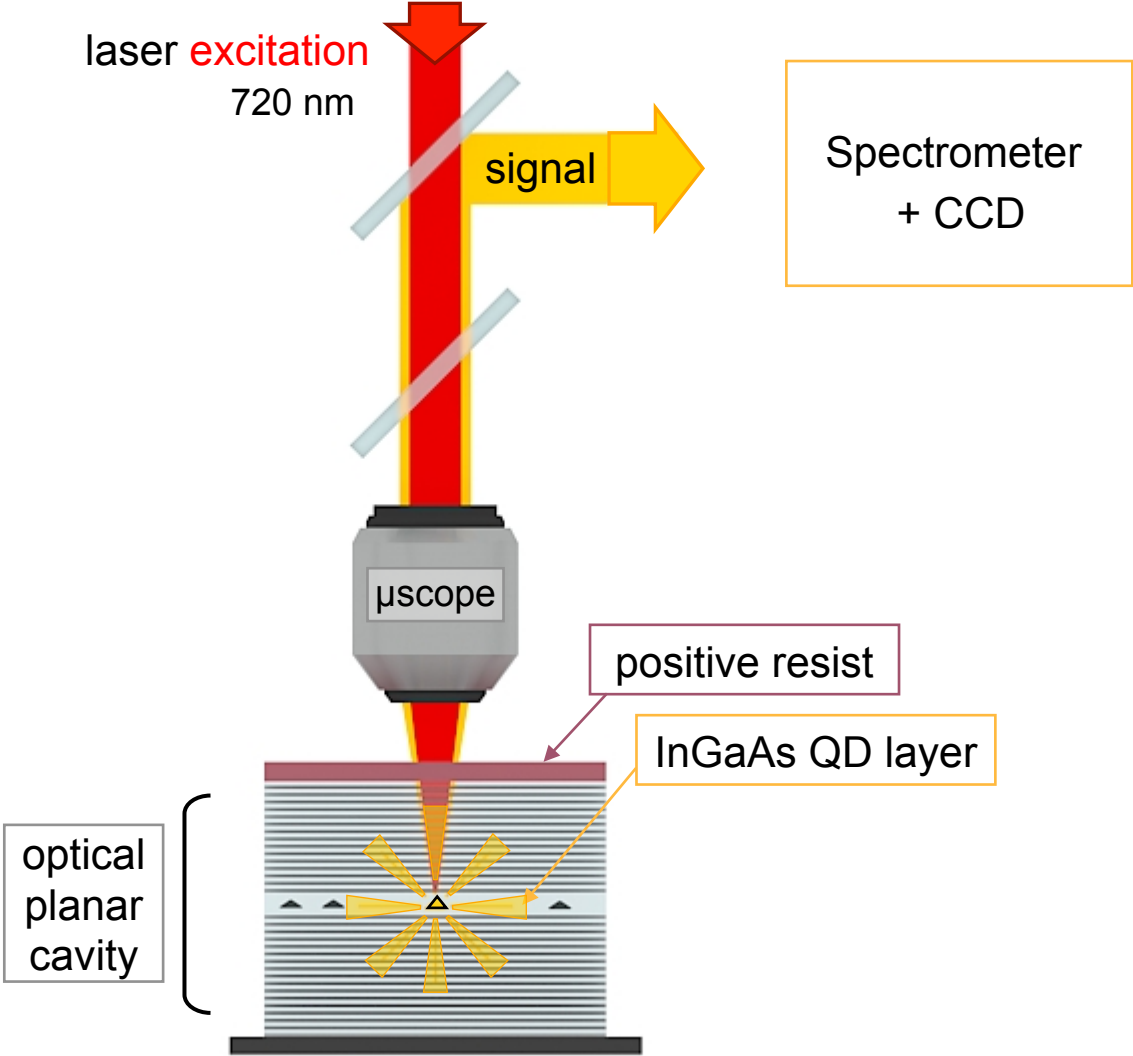
In situ lithography



In situ lithography

optical lithography
+ μ PL

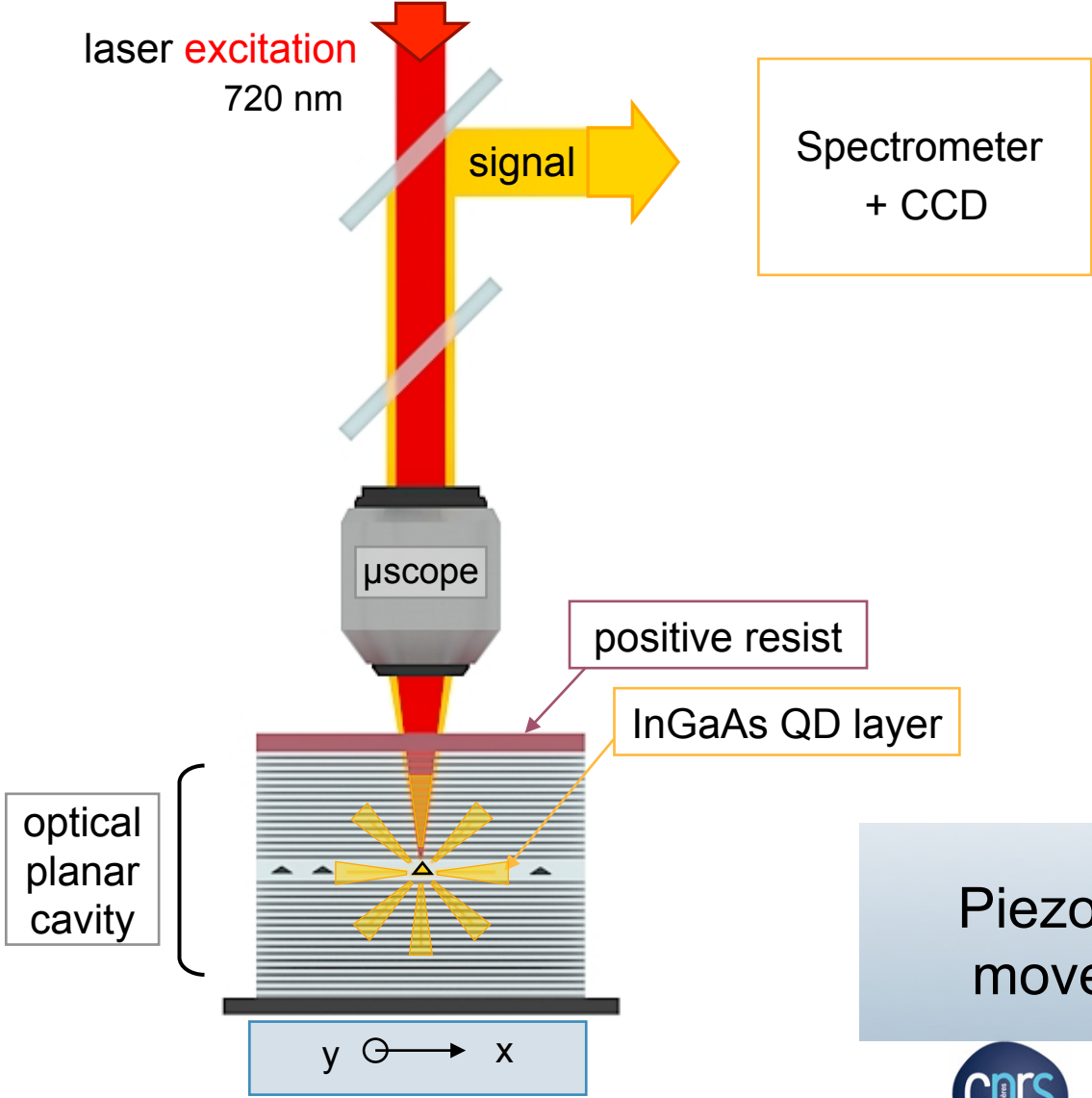
Cryostat
at 10 K



In situ lithography

optical lithography
+ μ PL

Cryostat
at 10 K



Piezoelectric
movements

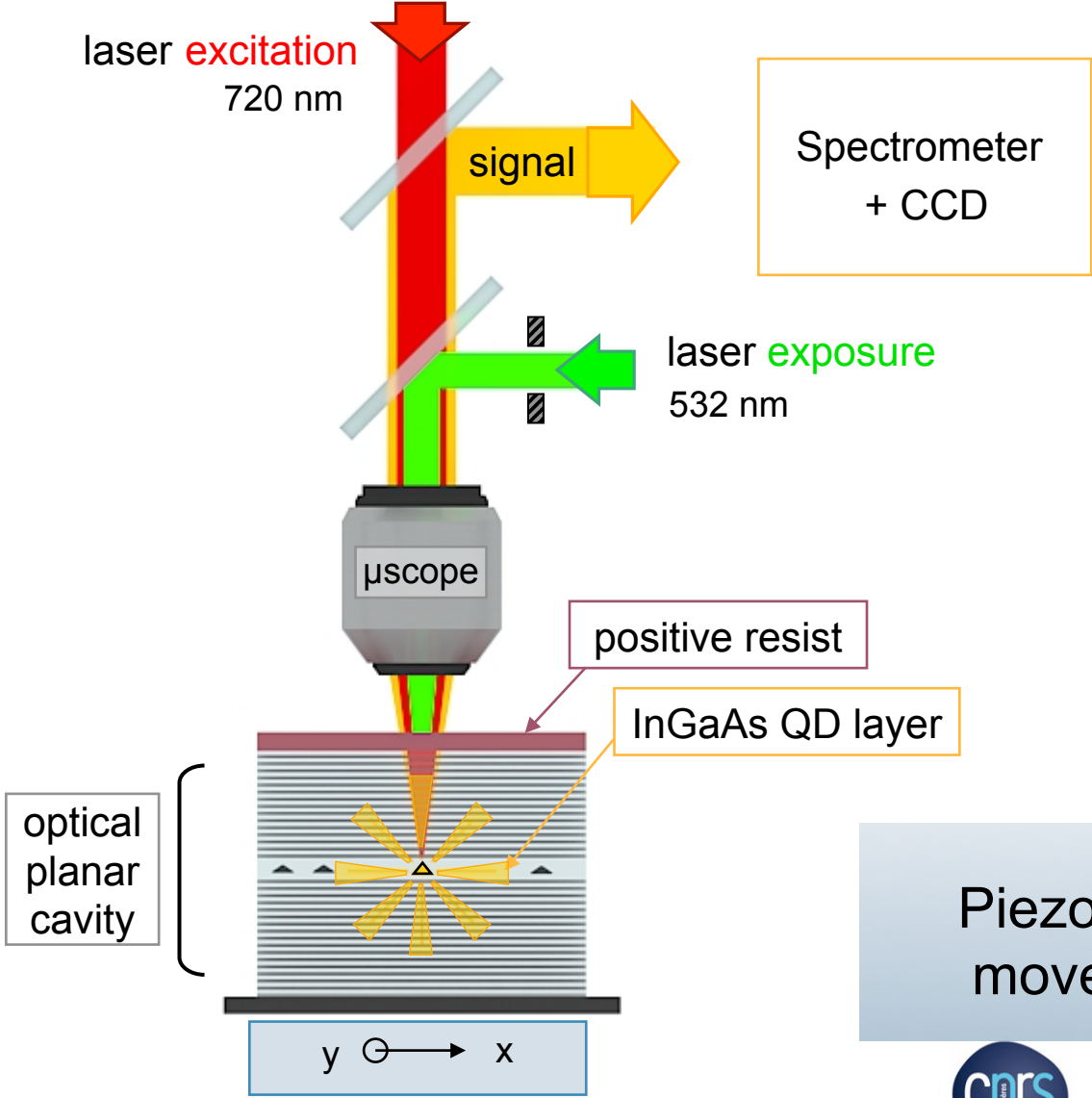


In situ lithography

optical lithography + μ PL

2 aligned lasers

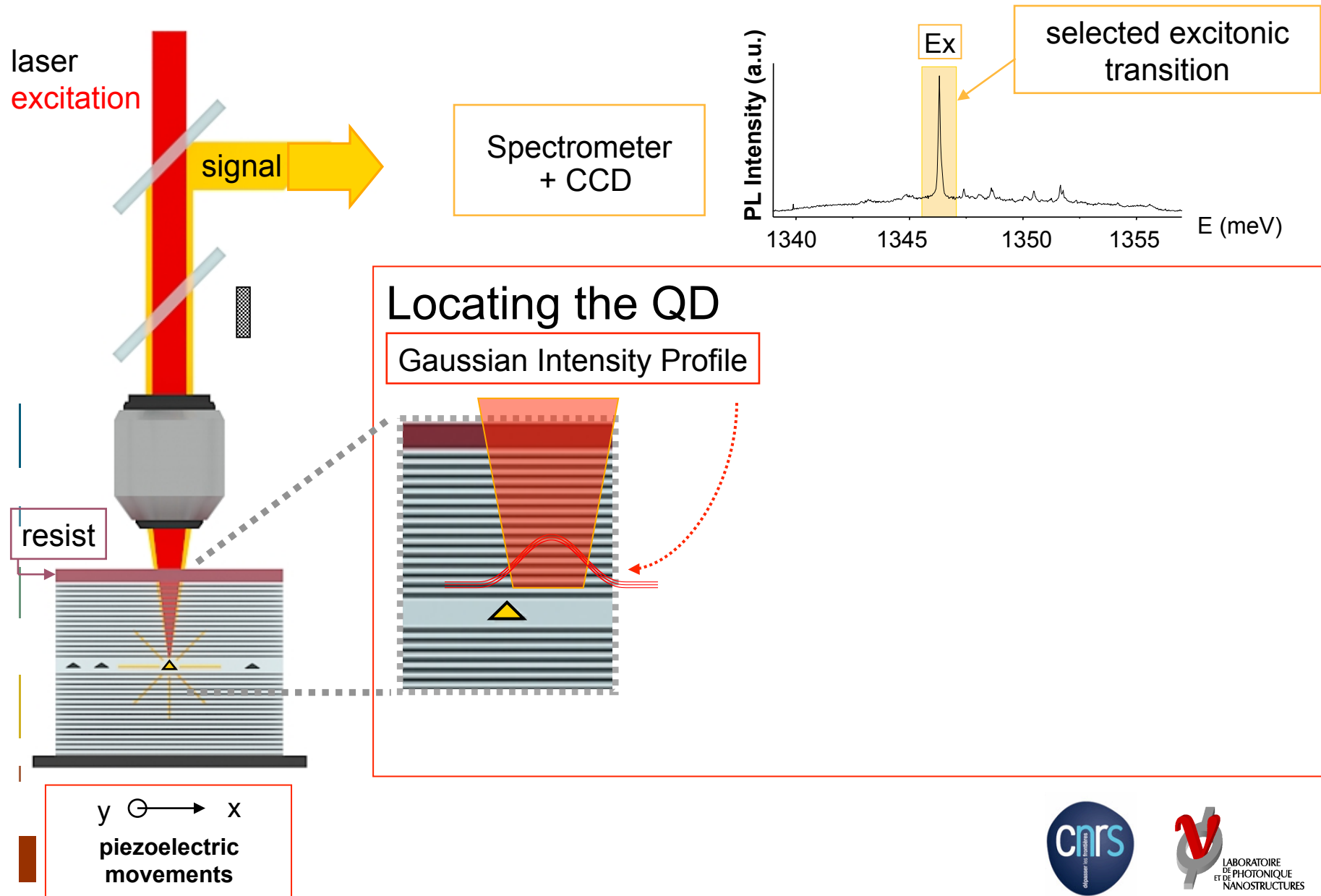
Cryostat at 10 K



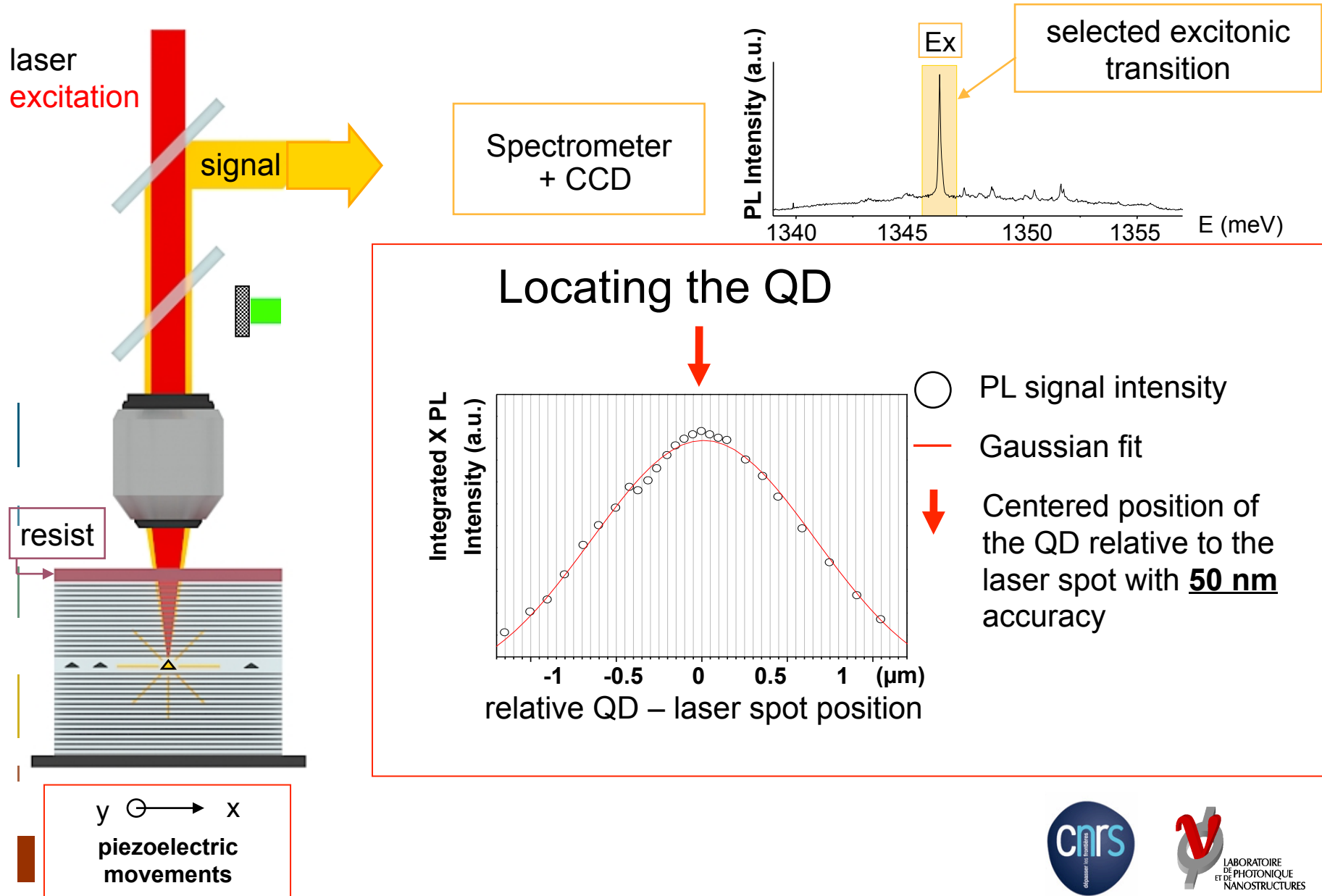
Piezoelectric movements



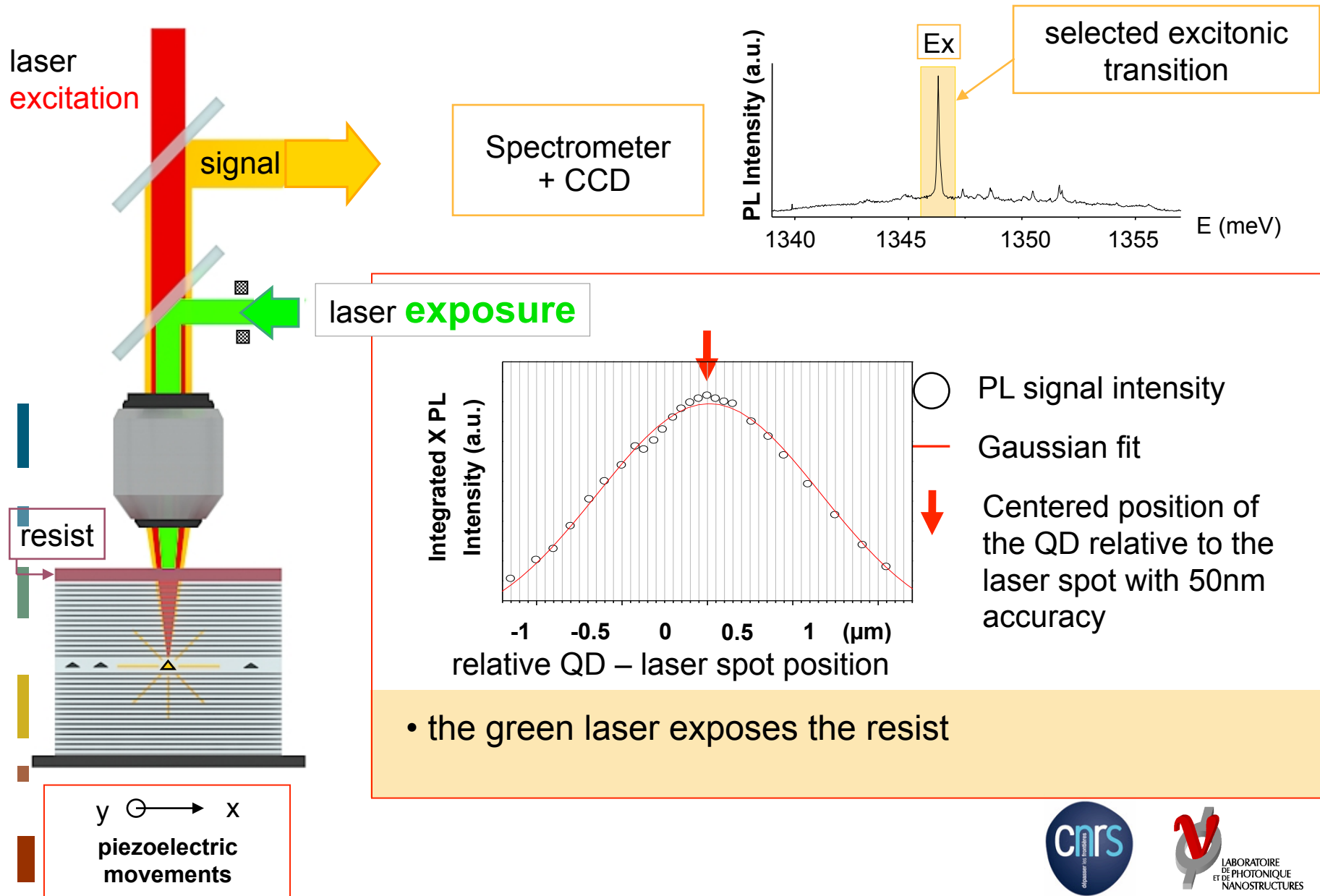
Spatial Matching



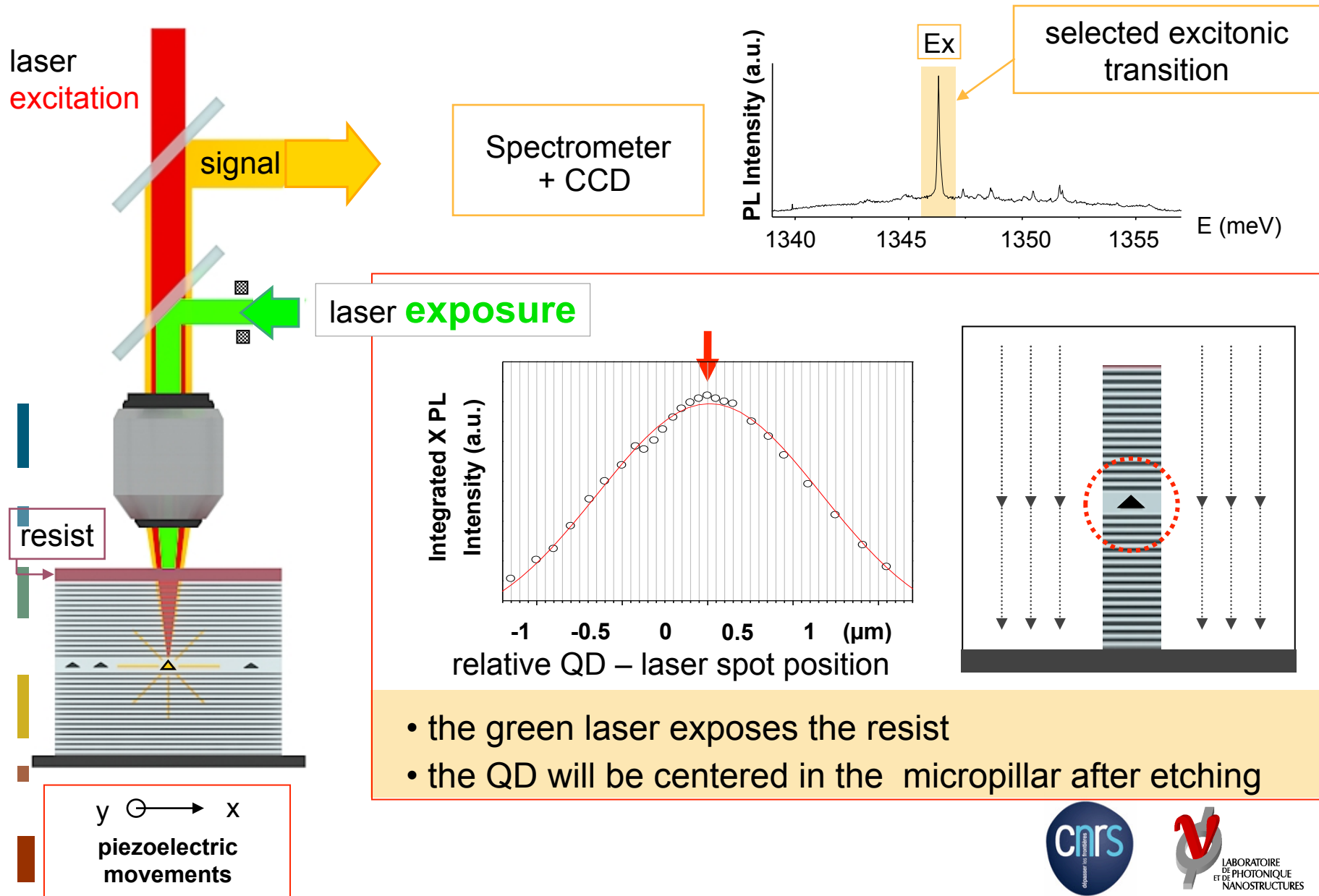
Spatial matching



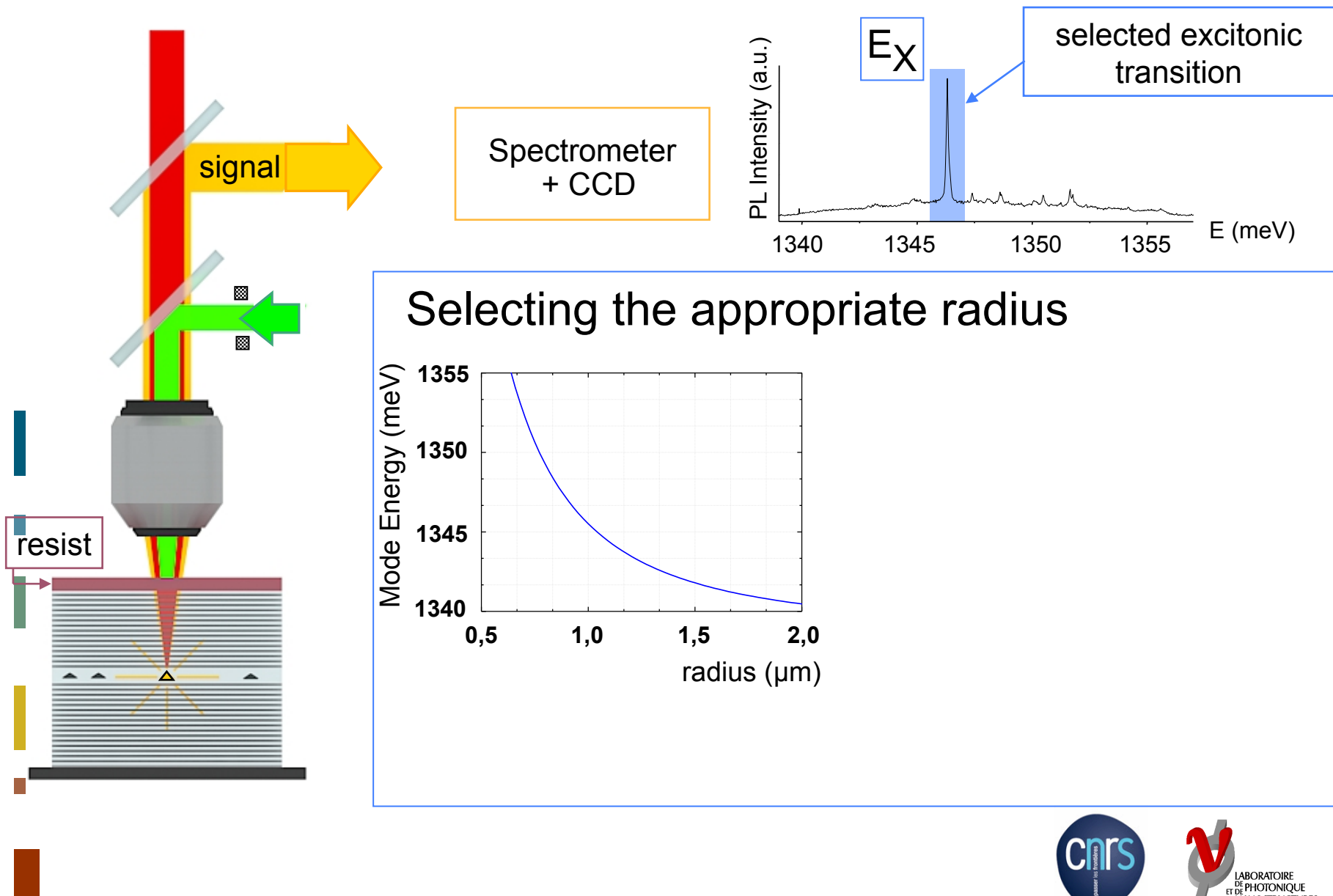
Spatial matching



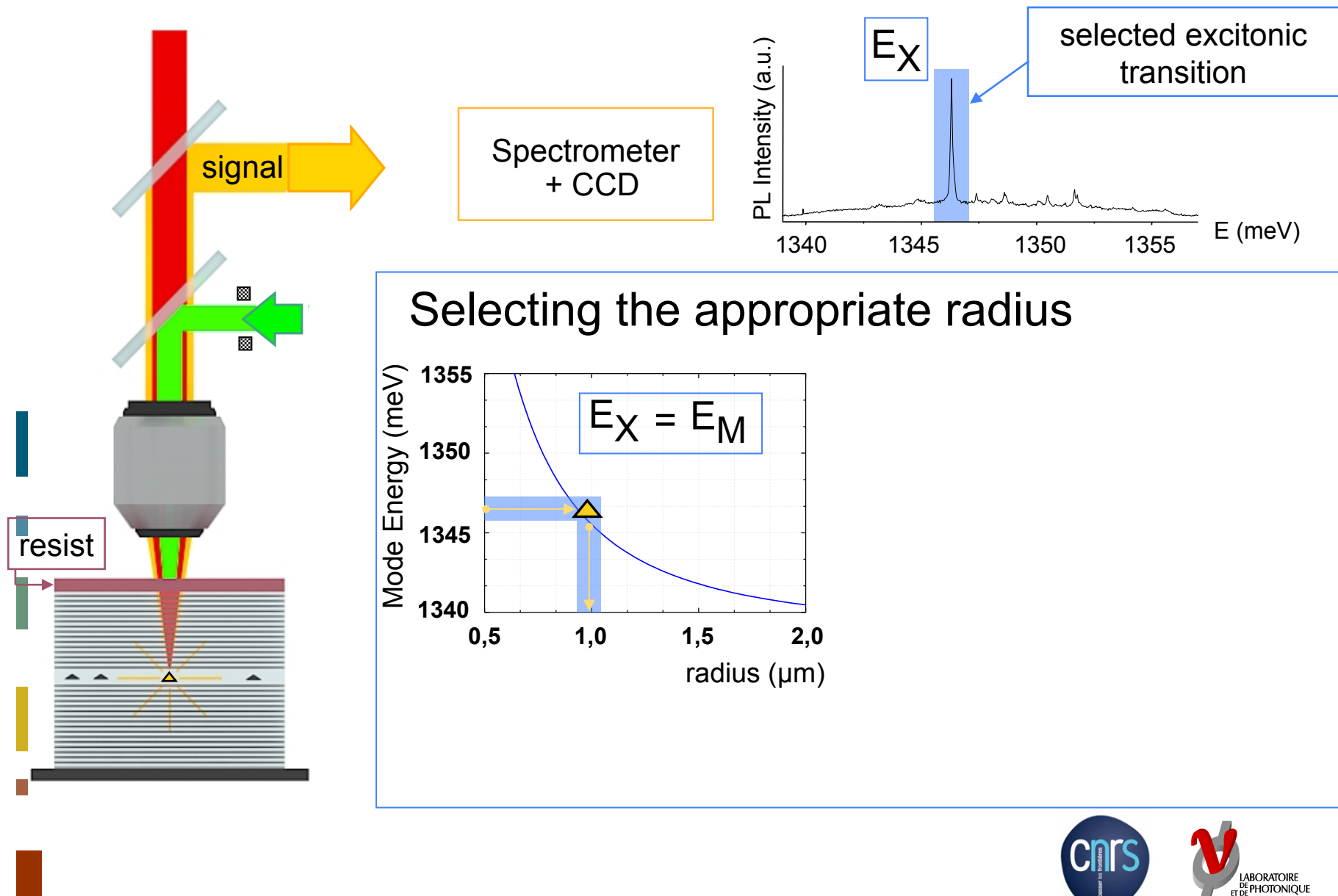
Spatial matching



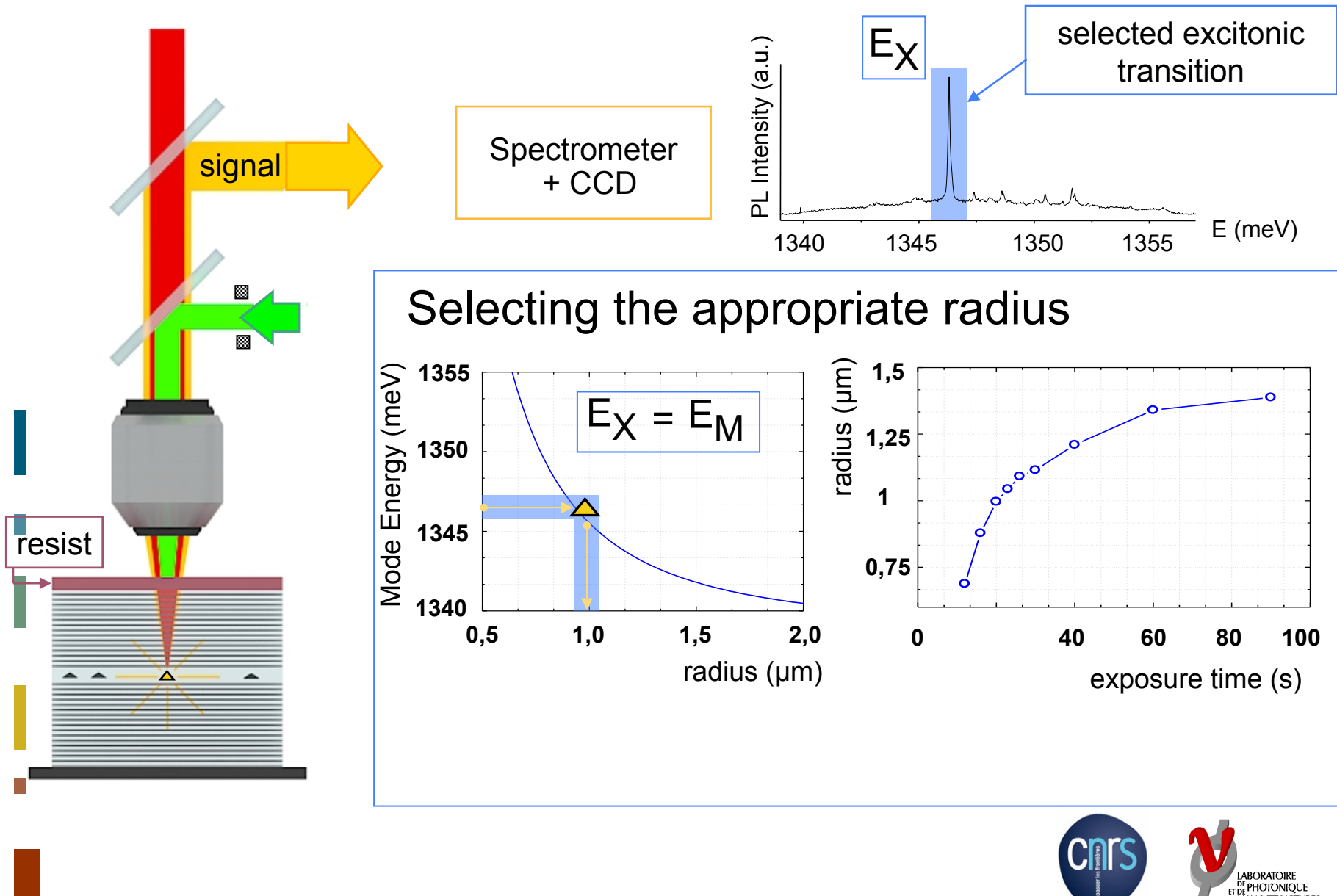
Spectral matching



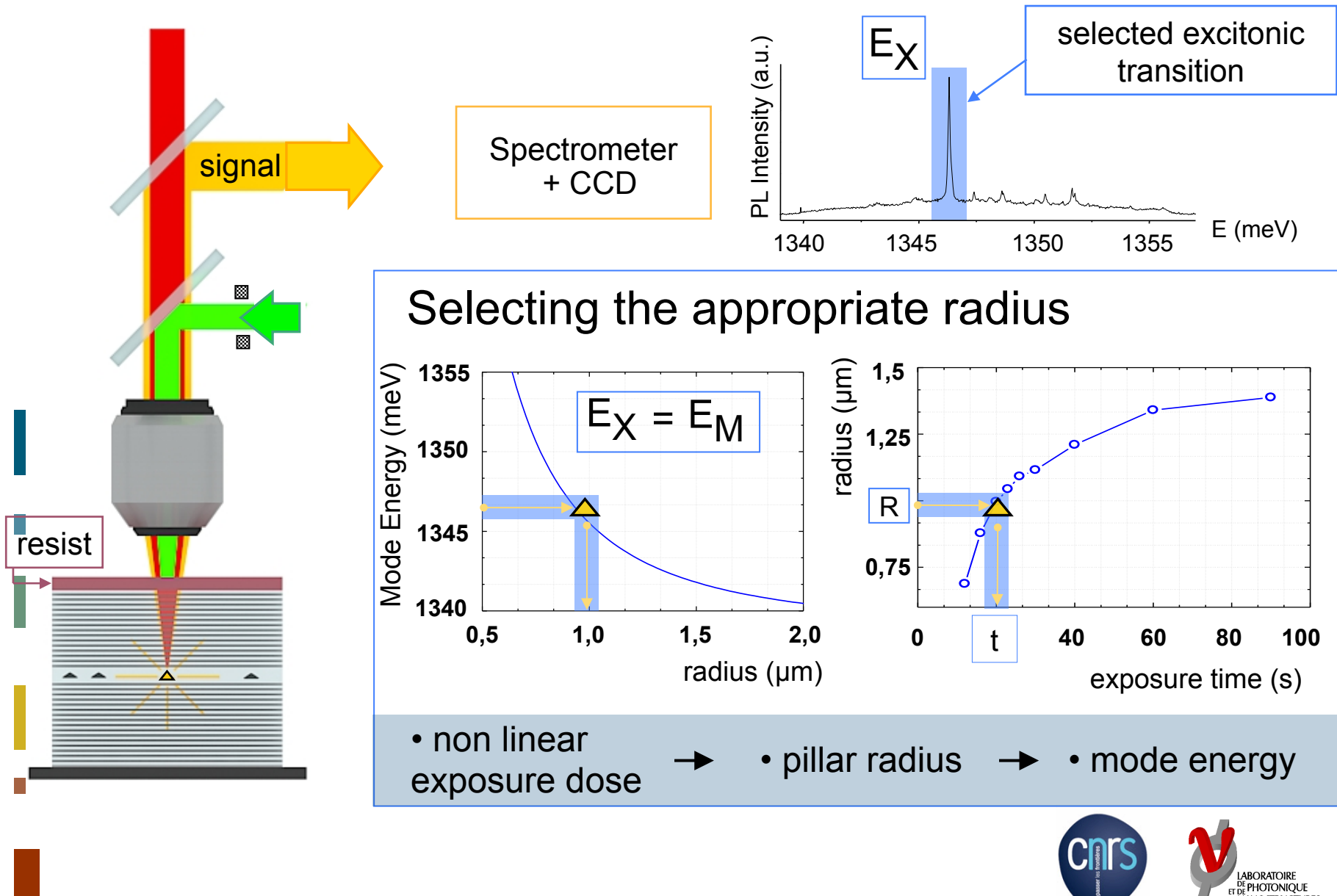
Spectral matching



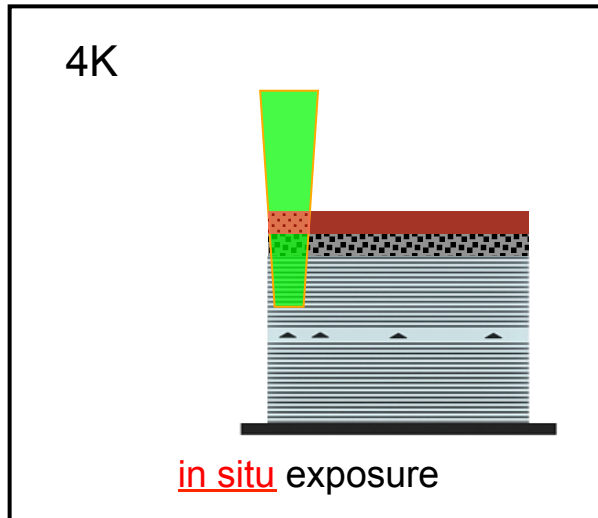
Spectral matching



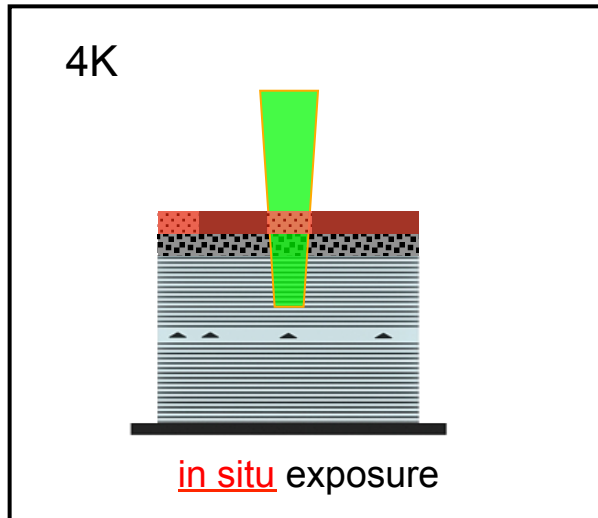
Spectral matching



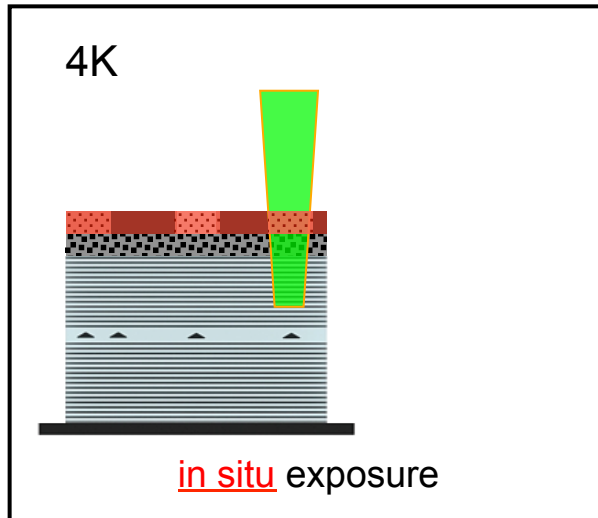
Post processing



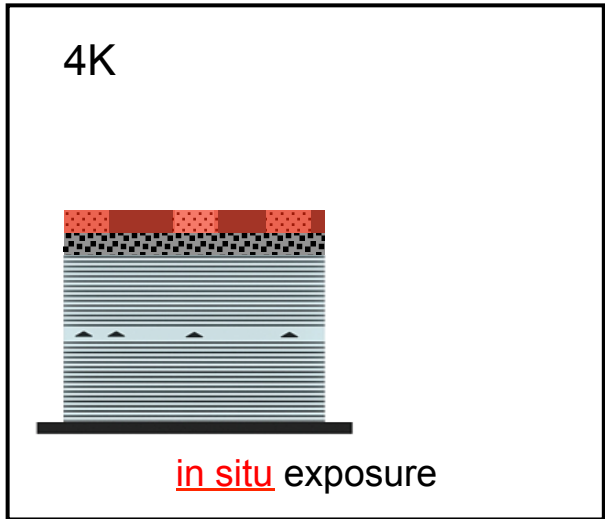
Post processing



Post processing

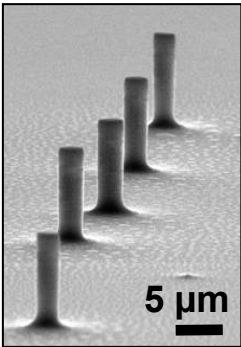
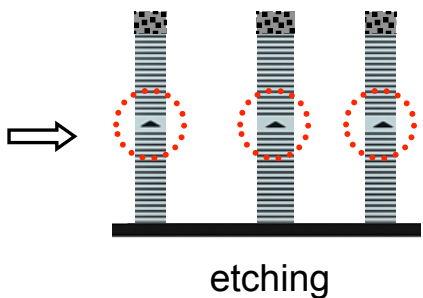
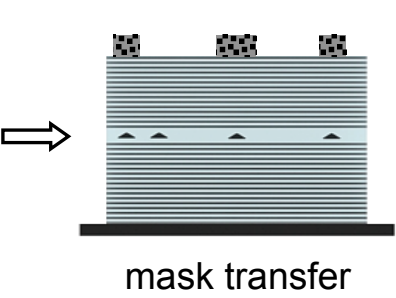
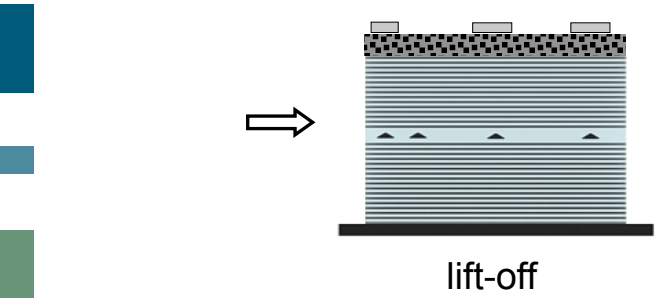
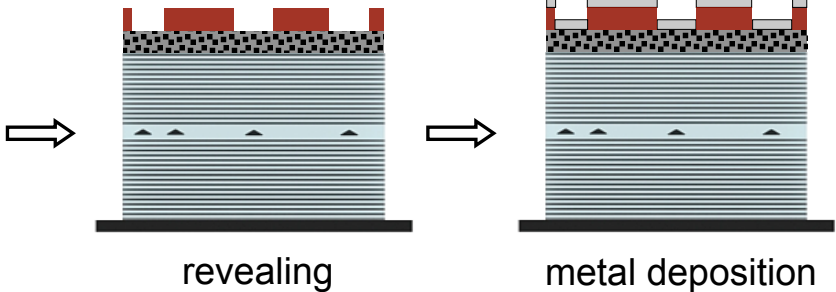


Post processing

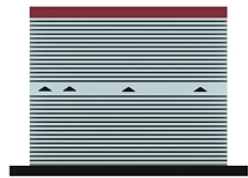


300 K

- metal
- resist
- PECVD Silicon Nitride



On demand weak coupling regime



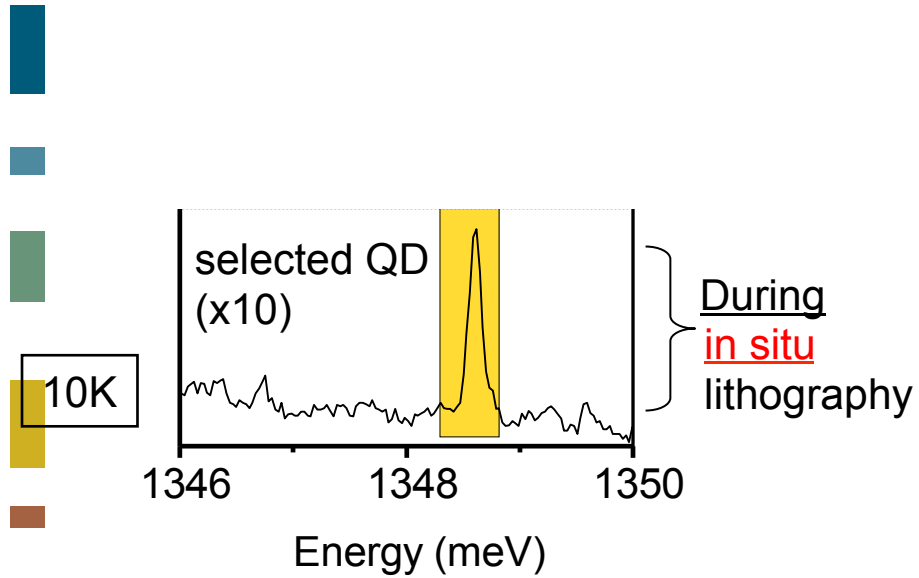
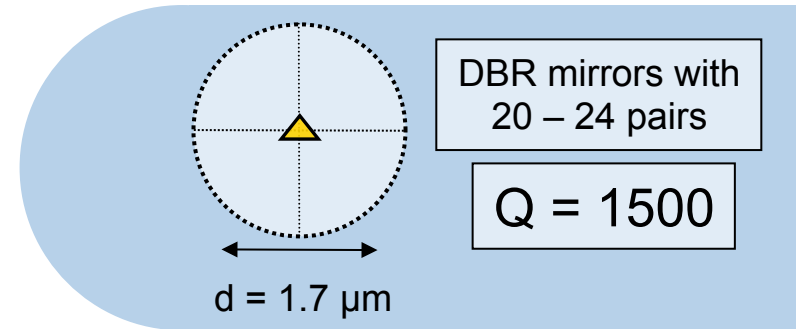
DBR mirrors with 20-24 pairs

Planar Cavity factor : $Q = 5000$

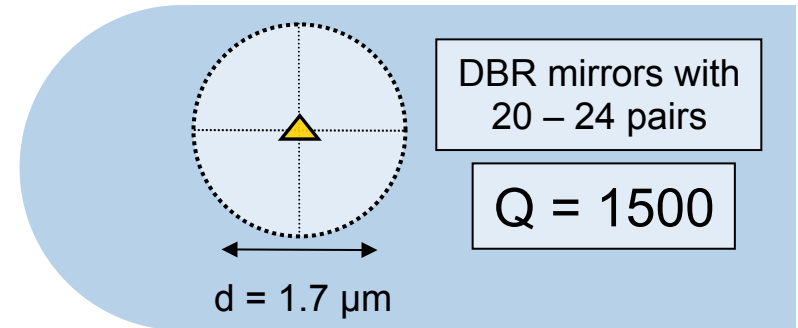
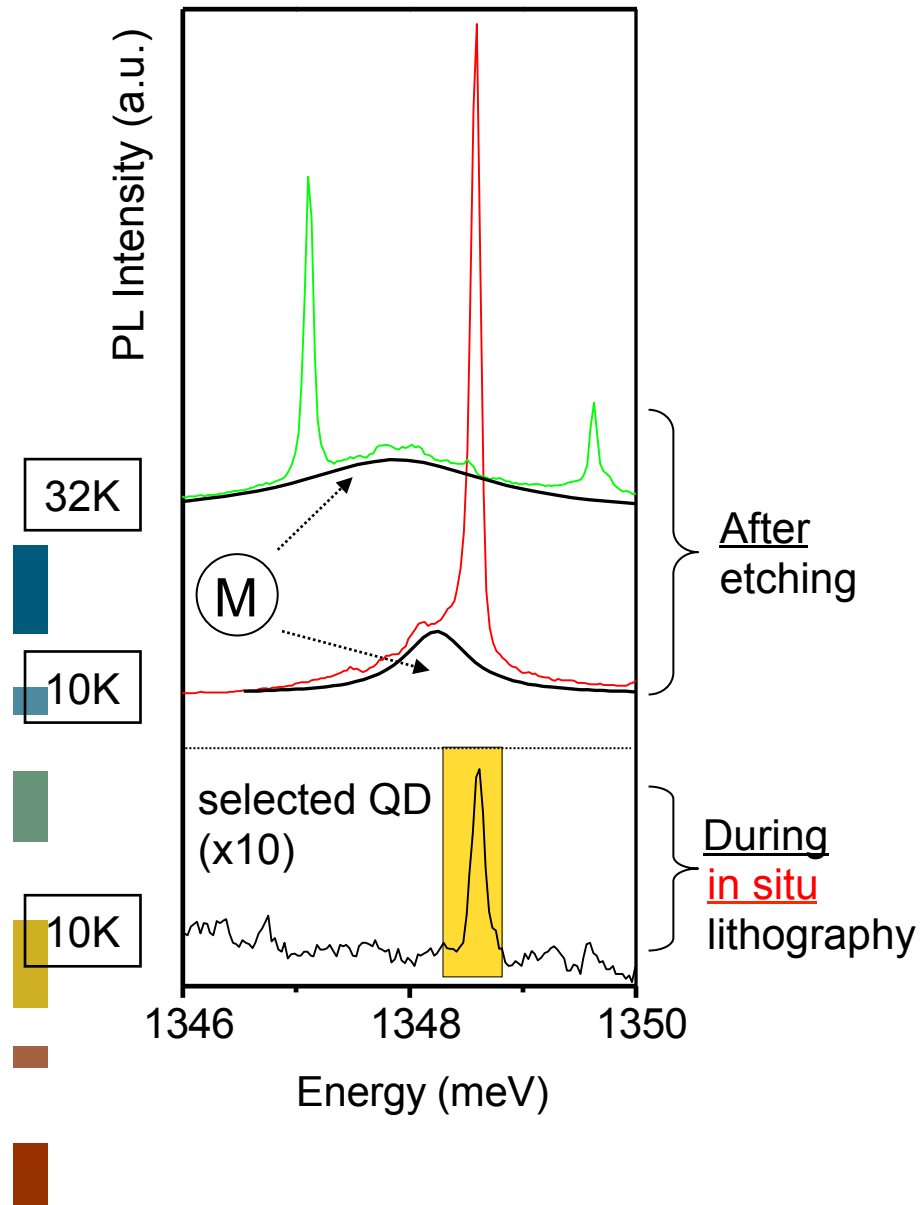
- A. Dousse, et al., *Phys. Rev. Lett.* **101**, 267404 (2008)
Research Highlight, Nature Materials **8**, 86 (2009)



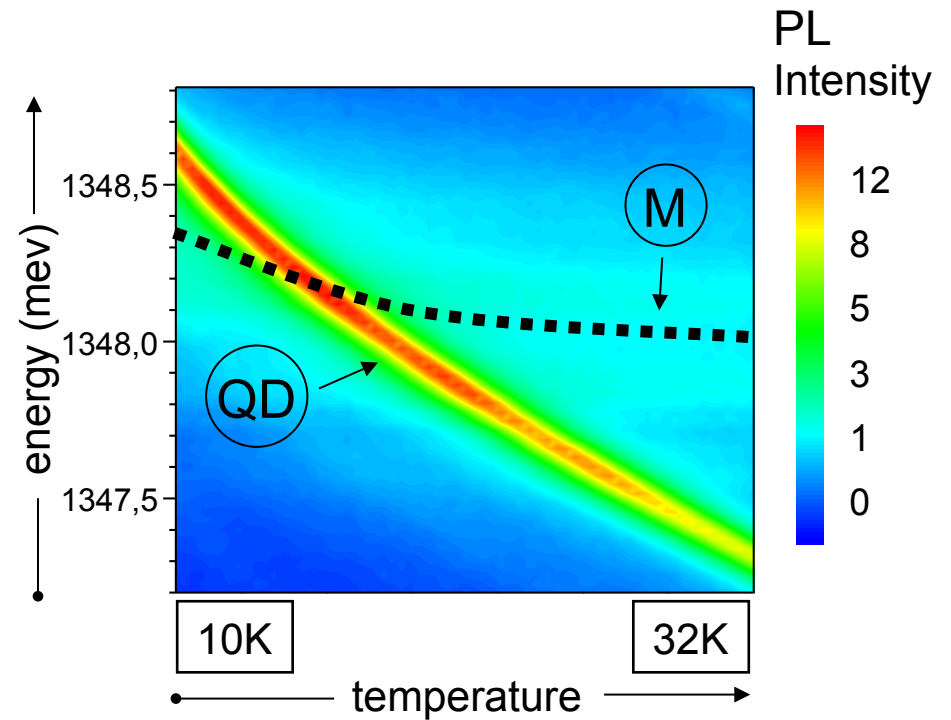
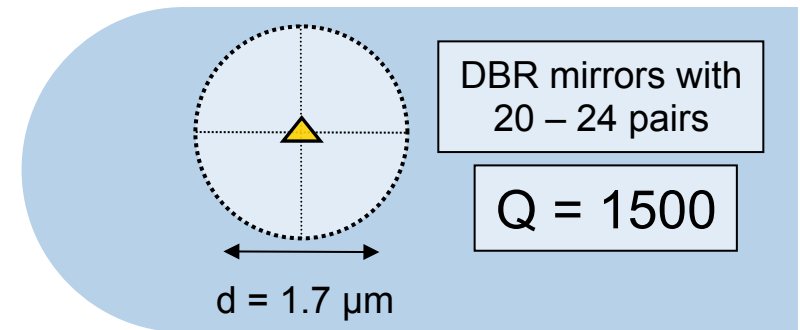
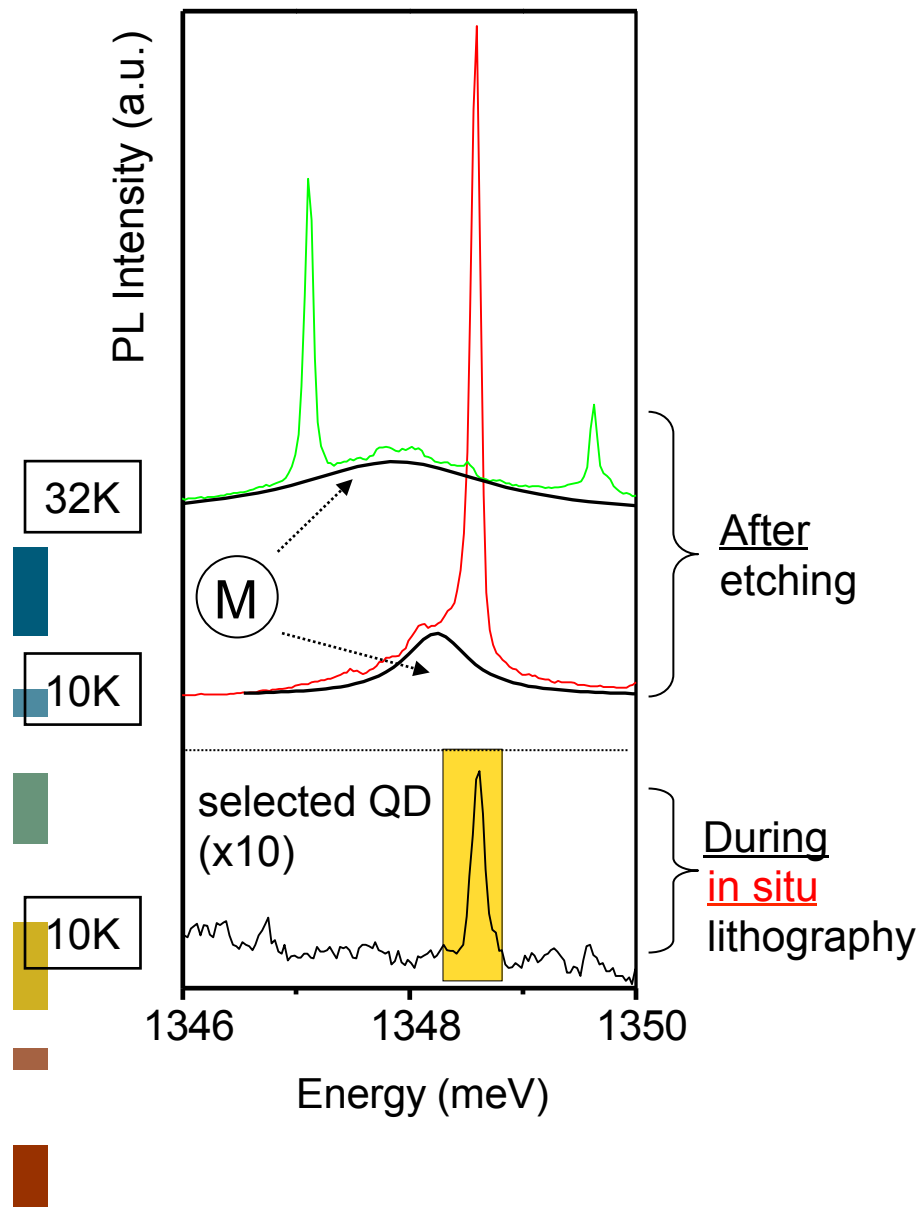
On demand weak coupling regime



On demand weak coupling regime

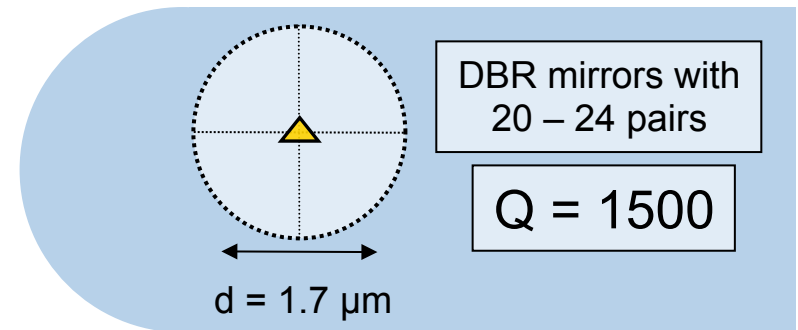
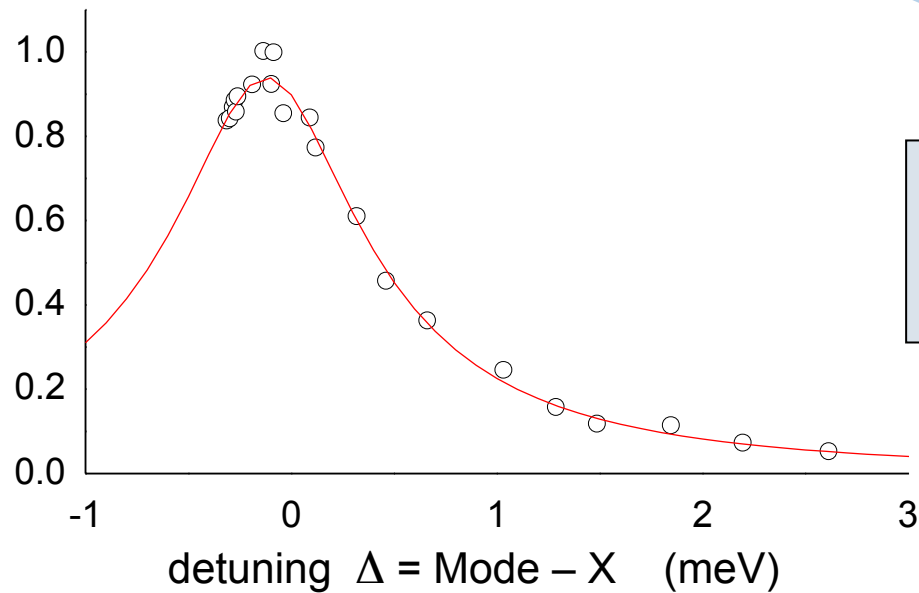


On demand weak coupling regime



On demand weak coupling regime

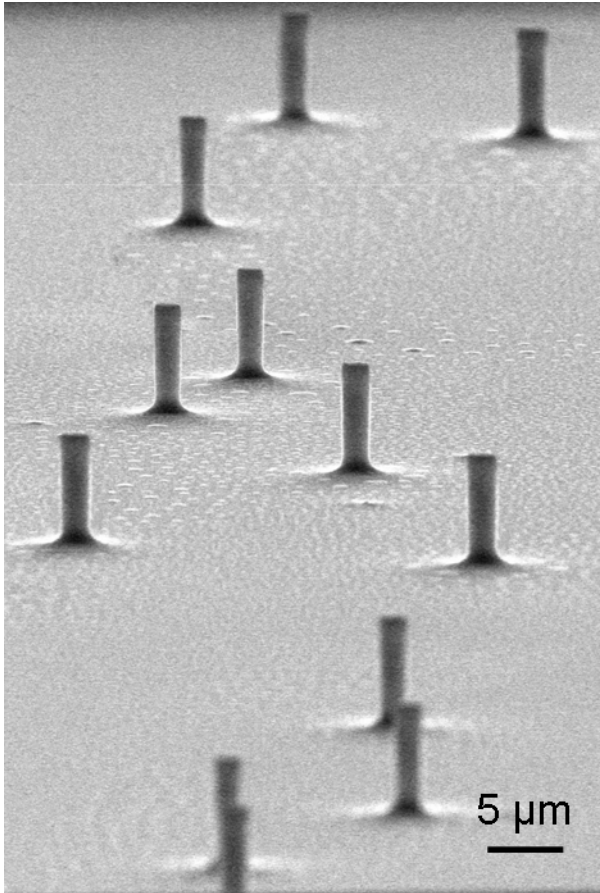
Normalised
PL intensity
at saturation



measured : $F_p = 9 \pm 3$
expected : $F_p = 9.5$

Good Spatial
Matching !

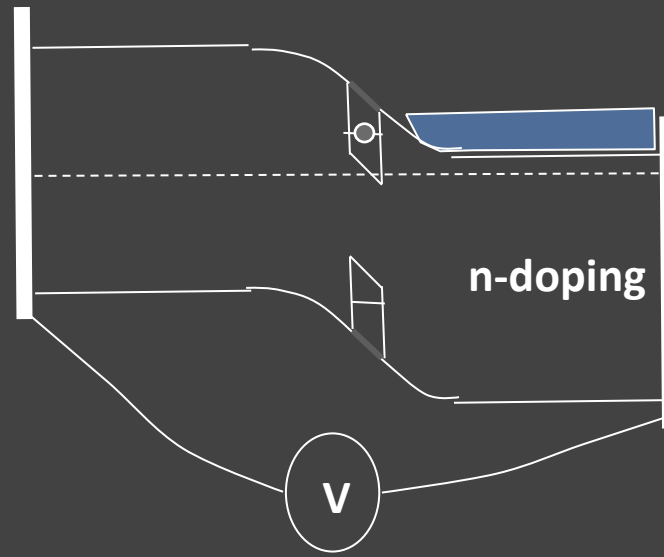
H. Lohmeyer et al., *Appl. Phys. Lett.* 92, 011116 (2008).



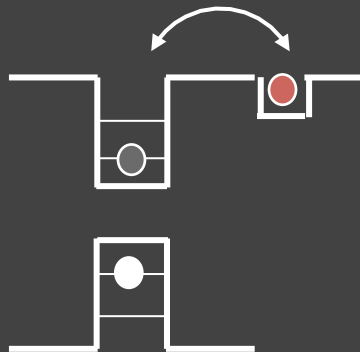
Around 40 pillars in one lithography process

- A. Dousse, et al., **Phys. Rev. Lett.** **101**, 267404 (2008)
Research Highlight, **Nature Materials** **8**, 86 (2009)

Electric control



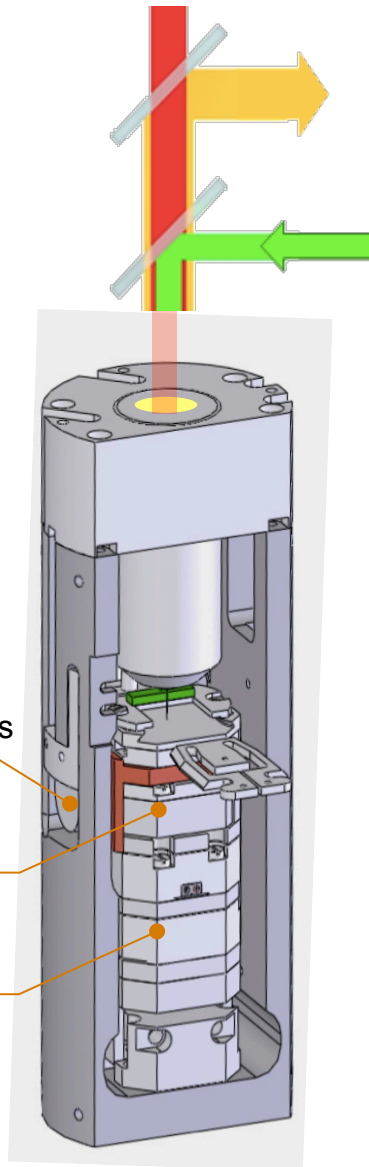
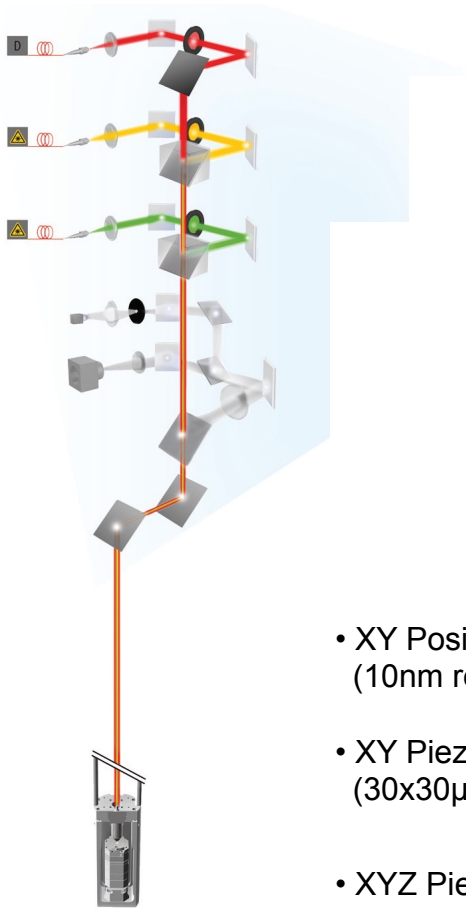
Reduce influence of *outside* residual charge



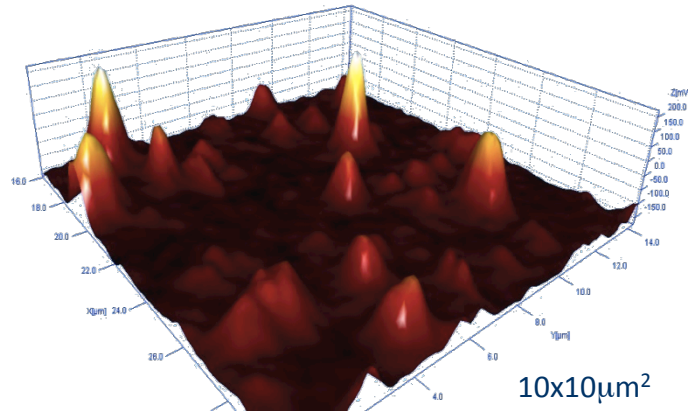
Control the charge *inside* the dot

Tune the QD emission energy

In situ optical lithography machine

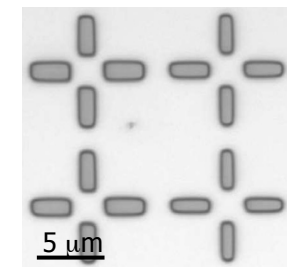
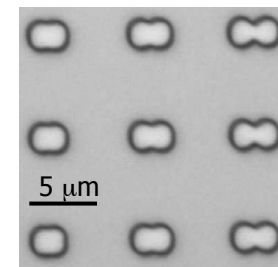


- XY Position sensors (10nm resolution)
- XY Piezo scanner (30x30 μm at 4K)
- XYZ Piezo stepper positioners (5x5x5 mm)



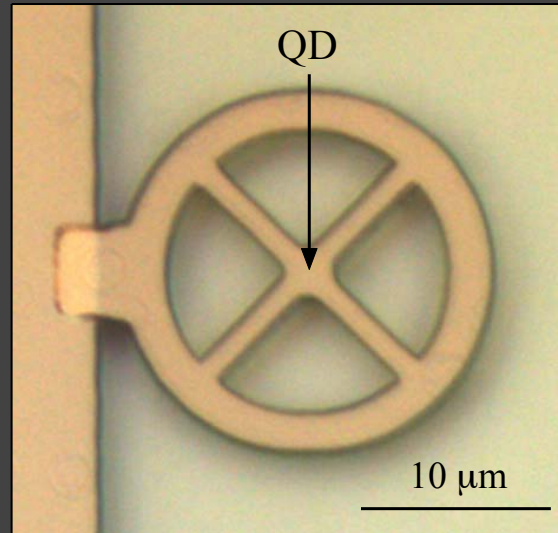
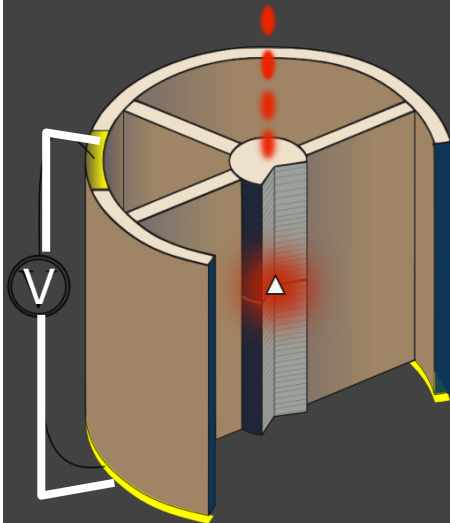
Absolute QD position
10 nm

Lithography patterns

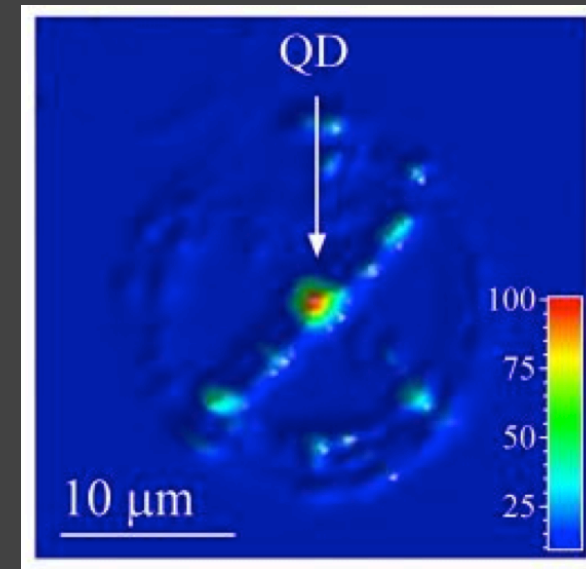


An electrical device

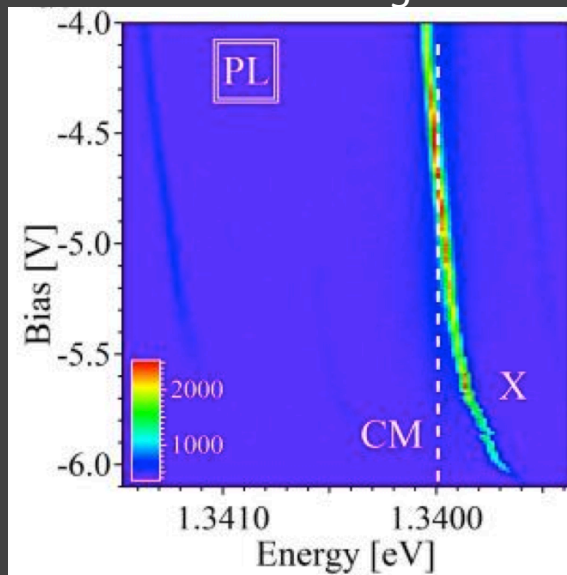
Optical microscope



Emission mapping



Emission tuning



Electrical control
Brightness > 55%

Nowak et al,
Nature Communication 2014

Conclusions



Material science does drive new fundamental studies